



# DIAGNOSTIC LINE RATIOS

VIII  
RVS Workshop  
Padova 2004

Federico Boschi

# Why diagnostic lines are important?

They are probes useful to investigate:

**Temperature**  
**(T)**

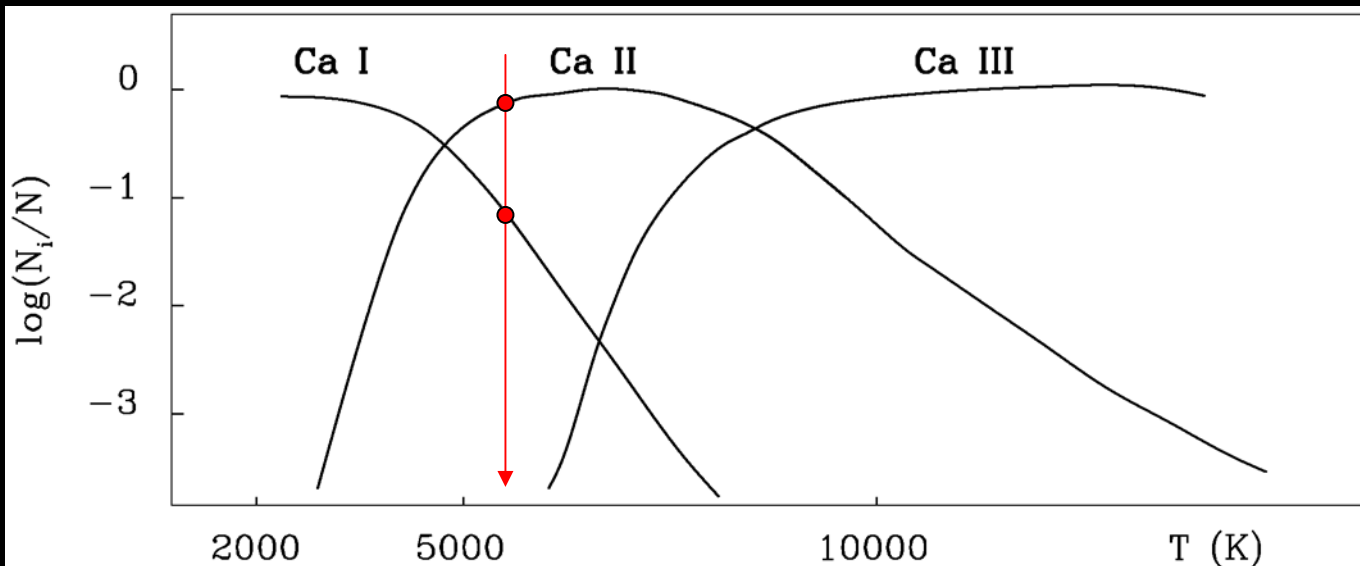
**Surface gravity**  
**(log g)**  
**Luminosity**

**CLASSIFICATION**  
**(temperature, luminosity)**

# TEMPERATURE

Best condition: two lines of the same element in two different ionized levels (ex. Ca I and Ca II).

CaI/CaII, Saha equation  $\rightarrow$  Temperature



Unfortunately in the GAIA region we can not find two lines with these characteristics.

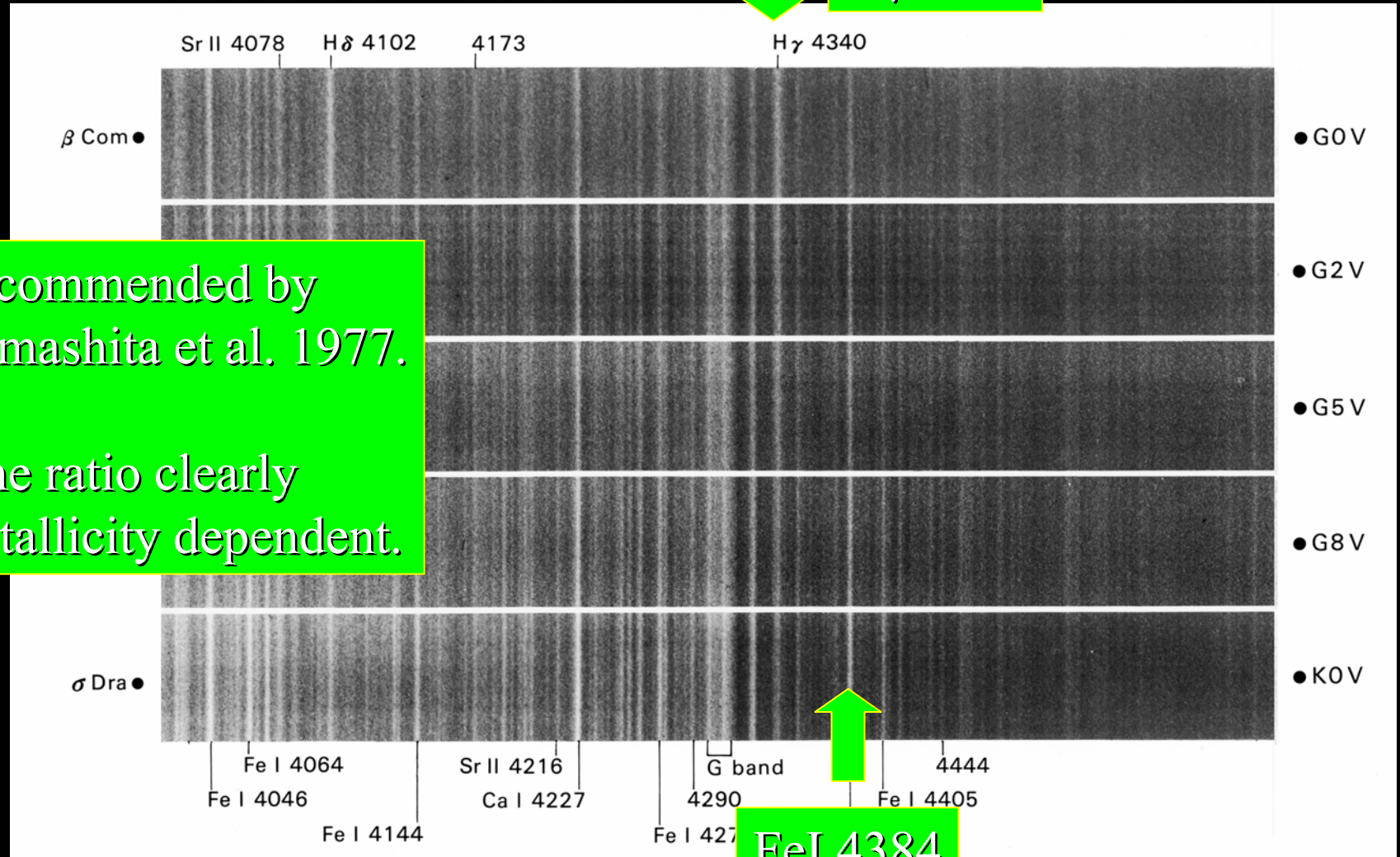
Temperature is derived from a visual comparison between two lines generally of different elements. The comparison is called *line ratio*.

Similar situation of the *Classical region*: 3600-4800 Å (MK Classif.)

# MK CLASSIFICATION

diagnostic line ratios for temperature

H $\gamma$  4340



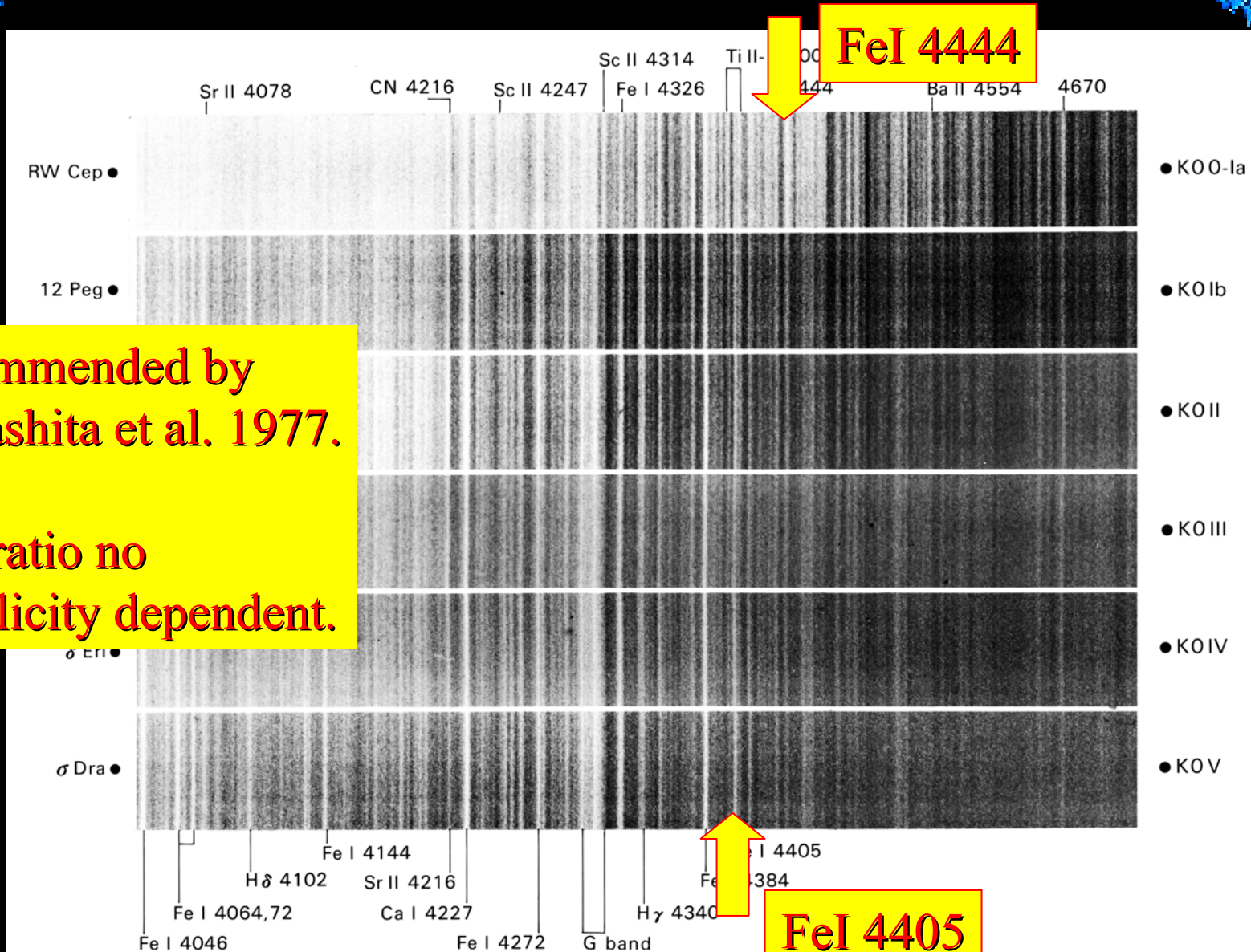
FeI 4384

Recommended by  
Yamashita et al. 1977.

Line ratio clearly  
metallicity dependent.

# MK CLASSIFICATION

diagnostic line ratios for luminosity



O4-B0	$\frac{\text{HeII } 4542}{\text{HeI } 4471}$		
O7-O9	$\frac{\text{HeII } 4200}{\text{HeI } 4026 + \text{HeI } 4144}$		
O7-B0	$\frac{\text{HeII } 4686}{\text{HeI } 4922}$		
B0-B0.5	$\frac{\text{SiIV } 4089 + \text{SiIV } 4116}{\text{HeI } 4121}$	$\frac{\text{HeII } 4686}{\text{HeI } 4713}$	
B0-B1	$\frac{\text{CIII } 4068-4070}{\text{HeI } 4009}$	$\frac{\text{CIII } 4647-4651}{\text{HeI } 4713}$	
B0-B2	$\frac{\text{SiIII } 4552}{\text{SiIV } 4089}$		
B1-B5	$\frac{\text{CII } 4267}{\text{MgII } 4481}$		
B3	$\frac{\text{SiII } 4128-4130}{\text{HeI } 4121}$		
B5-B7	$\frac{\text{CII } 4267}{\text{MgII } 4481}$	$\frac{\text{SiII } 4128-4130}{\text{HeI } 4144}$	
B5-A0	$\frac{\text{SiII } 4128-4131}{\text{HeI } 4144 + \text{HeI } 4026}$	$\frac{\text{MgII } 4481}{\text{HeI } 4471}$	profilo righe di Balmer
B9.5-A5	$\frac{\text{MnI } 4030-4034}{\text{FeI } 4271}$		
A0-A7	$\frac{\text{MgII } 4481}{\text{FeI } 4385}$		
A0-F0	$\frac{\text{CaII } 3934}{\text{CaI } 3968 + \text{HI } 3970}$		
F0-G0	$\frac{\text{FeI } 4046 \text{ o } \text{CaI } 4227}{\text{HI } 4102 \text{ o } \text{HI } 4340}$	$\frac{\text{MnI } 4030-4034}{\text{SiII } 4128-4132}$	$\frac{\text{CH4300}}{\text{FeI } 4385}$
G0-K0	$\frac{\text{FeI } 4046 \text{ o } \text{FeI } 4144 \text{ o } \text{CaI } 4227}{\text{HI } 4102}$	$\frac{\text{FeI } 4384}{\text{HI } 4340}$	$\frac{\text{FeI } 4921}{\text{HI } 4816}$

Diagnostic line ratios  
for  $T_{\text{eff}}$  recommended  
by Yamashita et al. 1977

A lot of diagnostic line ratios.

Each of them has a very  
small range of validity.

G0-K0

$$\frac{\text{FeI } 4046 \text{ o } \text{FeI } 4144 \text{ o } \text{CaI } 4227}{\text{HI } 4102}$$

$$\frac{\text{FeI } 4384}{\text{HI } 4340}$$

$$\frac{\text{FeI } 4921}{\text{HI } 4816}$$

M4-M8 banda CaOH 5500-5600

M7-M8 bande VO

O6-O8	<u>HeII 4686 e NIII 4634-4642 in emissione</u> NIV 3479-3485 in assorbimento					
O9-O9.5	<u>SiIV 4089</u> CIII 4068-4070	<u>SiIV 4116</u> HeI 4121	<u>CIII 4649</u> HeII 4686	<u>HeII 4686</u> CIII 4647-4651 + HeI 4713		
B0-B1	<u>SiIV 4119</u> HeI 4026,4144,4009	<u>SiIV 4116</u> HeI 4121	<u>SiIII 4553</u> HeI 4713			
B1	<u>SiIV 4089</u> HeI 4121	<u>YII 3983</u> FeI 4005	<u>FeI-CrII 4002</u> FeI 4005	<u>FeI-TiII 4025</u> FeI 4005,4046	<u>SrII 4078</u> FeI 4046	
	<u>OII-CIII</u> HeI 4713	<u>FeI 4179</u> FeI 4144	<u>FeI-TiII 4173</u> CaI 4227	<u>SrII 4216</u> CaI 4227		
B2	righe OII e <u>OII 4415</u> HeI 4121	<u>YII 3983</u> FeI 4005	<u>FeI-CrII 4002</u> FeI 4005	<u>FeI-TiII 4025</u> FeI 4005,4046	<u>SrII 4078</u> FeI 4046	<u>FeI 4179</u> FeI 4144
		<u>FeI-TiII 4173</u> CaI 4227 + FeI 4144	<u>SrII 4216</u> FeI 4144	<u>TiII 4444</u> MgII 4481	<u>Ball 4554</u> MgII 4481	
B3	<u>CII 3919</u> HeI 3965	<u>YII 3983</u> FeI 4005	<u>FeI-TiII 4025</u> FeI 4005	<u>SrII 4078</u> HI 4102 + FeI4046	<u>FeI 4129,4179</u> FeI 4144	
	<u>CII 4227</u> HeI 4388	<u>SrII 4126 + ScII 4247</u> FeI 4144	<u>Ball 4554</u> MgII 4481			
B5-B7	<u>HeI 3965</u> HeI 4009	<u>YII 3983</u> FeI 4005	<u>SrII 4078</u> HI 4102 + FeI 4046,4064	<u>FeI 4179</u> FeI 4173	<u>SrII 4216</u> FeI 4144	
	profilo righe					
B7-B8	ali delle righe	<u>G5-G8</u>	<u>SrII 4078</u> CaI 4227 + FeI 4046,4064	<u>SrII 4216</u> FeI 4144,4272 + CaI4226	<u>TiII 4400,4408</u> FeI 4405	
A0-A2	<u>SiII 3856</u> CaII 3933	<u>G8-K0</u>	discontinuità di CN a 4216	<u>SrII 4078</u> FeI 4046,4064,4072	<u>TiII 4400,4408</u> FeI 4405	<u>FeI 4444</u> FeI 4405
A2-A3	...	<u>K2-K4</u>	discontinuità di CN a 4216	<u>SrII 4078</u>	<u>HI 4012</u>	

Diagnostic line ratios for log g recommended by Yamashita et al. 1977.

<b>G8-K0</b>	discontinuità di CN a 4216	<u>SrII 4078</u> FeI 4046,4064,4072	<u>TiII 4400,4408</u> FeI 4405	<u>FeI 4444</u> FeI 4405
--------------	----------------------------	--	-----------------------------------	-----------------------------

	<u>FeI 4064,4072</u>	<u>FeI 4064,4072,4144</u>	<u>FeI 4144 + TiI 4186</u>		
<u>FeI-TiI</u>	<u>M0-M1</u>	<u>SrII 4078</u> FeI 4046,4064	<u>HI 4012</u> FeI 4144	<u>SrII-FeI 4216</u> FeI 4144	<u>FeI 4375,4389</u> FeI 4384
	<u>M1-M4</u>	<u>SrII 4078</u> FeI 4046,4064,4072,4263	<u>HI 4012</u> FeI 4046,4144	<u>SrII-FeI 4216</u> FeI 4144,4251	<u>FeI 4375,4389</u> FeI 4384

# MK CLASSIFICATION

the state of the art

- A lot of diagnostic line ratios.
- Small range of validity for each of them.

No numerical relations between diagnostic lines  
and physical parameters:

*“...a line is deeper than the another line...”*  
*“...the line intensity increases with temperature...”*





I.  
GAIA WAVELENGTH RANGE  
8500-8750 Å

*ANOVA + SYNTHETIC SPECTRA*

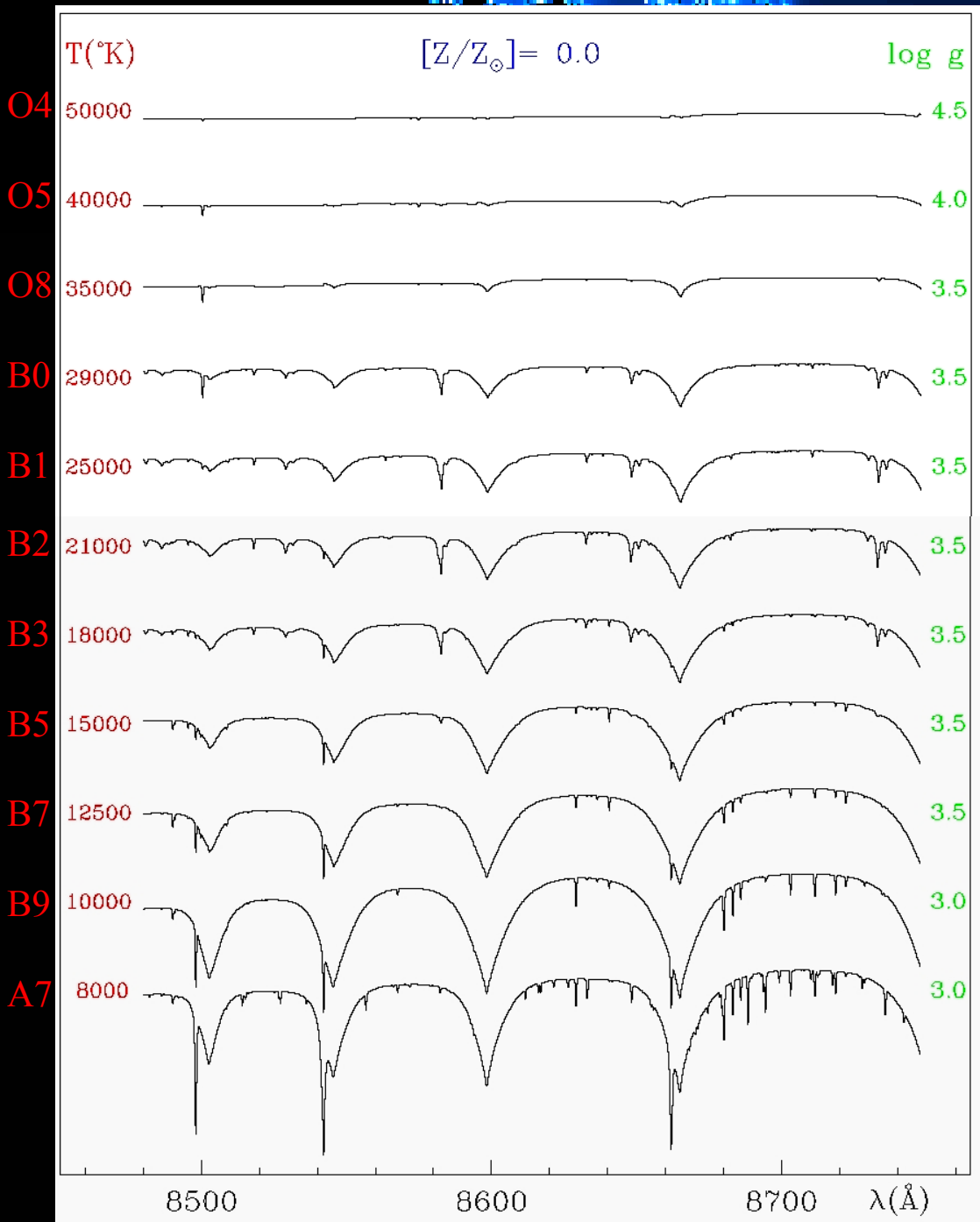
*To identify the lines sensitive to the physical parameters (temperature and log g) we used a statistical method ANOVA + Synthetic Kurucz Spectra (solar metallicity).*

$$\text{Line depth} = A(T) + B(\log g) + AB(T, \log g) + W(\text{constant})$$

Behaviour of 170 lines depending on temperature and/or luminosity.

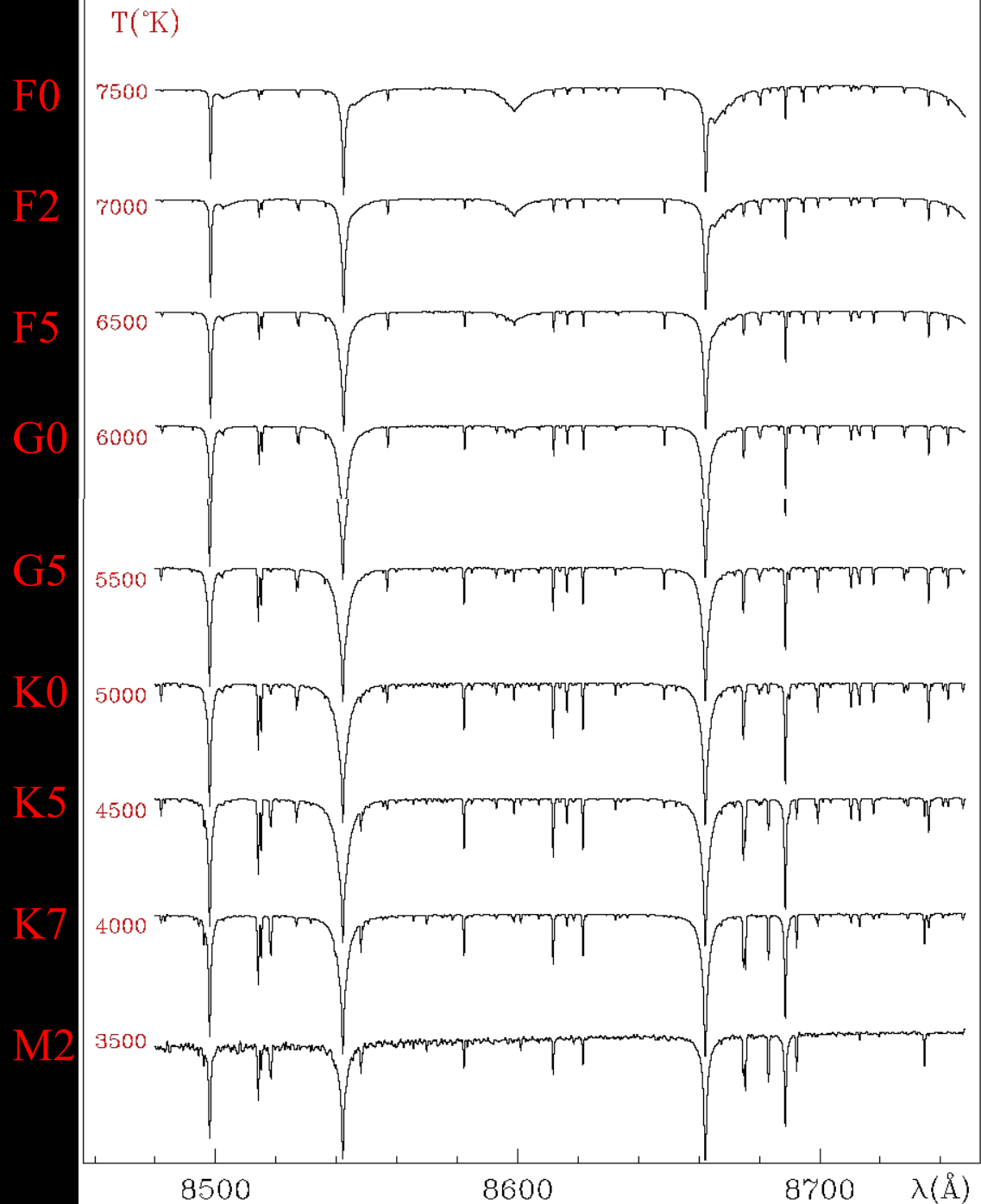
Synthetic spectra  
in the GAIA region  
for stars O4-A7.

From Castelli & Munari,  
2001, A&A 366, 1003  
and  
Zwitter, Castelli & Munari  
2004, A&A 417, 1055



Synthetic spectra  
in the GAIA region  
for stars F0-M2.

From Munari & Castelli,  
2000, A&AS 141, 141  
and  
Zwitter, Castelli & Munari  
2004, A&A 417, 1055



$n^{\circ} pix$	$\lambda(\text{\AA})$ □	ID	$n^{\circ} mult.$	<i>thesis</i>	A ■	B □	AB	W
5859	8601.052	FeI			0.2302	0.0905	0.0376	0.0145
5859	8601.079	TiI			0.2302	0.0905	0.0376	0.0145
6507	8713.187	FeI	400/1267	<b>g</b>	0.2423	0.0233	0.0710	0.0092
6507	8713.210	FeI			0.2423	0.0233	0.0710	0.0092
6249	8668.440	SiI			0.2457	0.1264	0.0245	0.0128
5534	8545.387	HI	10 (P15)	<b>0; a</b>	0.2521	0.7051	0.1916	0.0372
5550	8548.098	TiI	150		0.2763	0.2238	0.0307	0.0215
6213	8662.141	CaII	2		0.3064	0.2067	0.0026	0.0116
5829	8595.960	SiI	80		0.3136	0.0893	0.0342	0.0115
5277	8501.544	SiI			0.3432	0.2609	0.1075	0.0182
5374	8517.971	TiI	182		0.3720	0.0485	0.0264	0.0175
5283	8502.487	HI	10 (P16)		0.3754	0.8509	0.1569	0.0394
5284	8502.668	FeI			0.3806	0.7968	0.1566	0.0389
5846	8598.825	FeI	1153		0.4076	0.4968	0.1187	0.0299
5279	8501.799	NiI			0.4220	0.3637	0.1475	0.0234
6630	8734.707	TiI	68	<b>dh</b>	0.4388	0.0125	0.0389	0.0227
6211	8661.898	FeI			0.4585	0.2476	0.0042	0.0166
5836	8597.050	SiI	80		0.4675	0.2109	0.0693	0.0211
5281	8502.219	SiI			0.5009	0.5386	0.1755	0.0296
5357	8515.110	FeI			0.5451	0.0460	0.0369	0.0126
5750	8582.257	FeI	401	<b>e</b>	0.5555	0.0333	0.0458	0.0127
5376	8518.349	TiI	150	<b>5; b</b>	0.5645	0.0416	0.0230	0.0195
6387	8692.326	TiI	68		0.5821	0.0118	0.0417	0.0203
6286	8674.743	FeI	339		0.6130	0.0238	0.0420	0.0133
6230	8665.022	HI	9 (P13)		0.6274	0.5752	0.1553	0.0370
5978	8621.598	FeI	401		0.6374	0.0221	0.0515	0.0129
5921	8611.795	FeI	339		0.6875	0.0308	0.0597	0.0166
6333	8682.988	TiI	68	<b>2; f</b>	0.8372	0.0170	0.0321	0.0196
5844	8598.396	HI	9 (P14)	<b>1; a</b>	1.0008	0.6333	0.2313	0.0402
6289	8675.374	TiI	68	<b>7</b>	1.0124	0.0198	0.0297	0.0207
5351	8514.069	FeI	60	<b>5; b</b>	1.0297	0.0331	0.0276	0.0174
5842	8598.191	TiI			1.0413	0.5302	0.2349	0.0393
6366	8688.621	FeI	60	<b>34; c</b>	1.6252	0.0006	0.0286	0.0268

**RESULTS**  
from ANOVA  
for temperature

Lines arranged  
in order of  
sensitivity to  $T_{\text{eff}}$   
(A coefficient).

The most sensitive  
lines are FeI, TiI  
and Paschen lines.

$n^{\circ} \text{pix}$	$\lambda(\text{\AA})$ □	ID	$n^{\circ} \text{mult.}$	<i>thesis</i>	A □	B ■	AB	W
6317	8680.282	NI	1		0.1297	0.1167	0.0041	0.0064
6318	8680.411	SI			0.1941	0.1172	0.0132	0.0072
6249	8668.440	SI			0.2457	0.1264	0.0245	0.0128
5245	8496.108	TiI			0.1521	0.1338	0.0116	0.0151
5555	8548.877	CrI			0.0667	0.1535	0.0217	0.0124
5247	8496.483	FeI			0.0204	0.1610	0.0145	0.0123
6243	8667.363	FeI			0.1428	0.1892	0.0311	0.0166
6243	8667.380	SiI			0.1428	0.1892	0.0311	0.0166
6213	8662.141	CaII	2		0.3064	0.2067	0.0026	0.0116
5836	8597.050	SiI	80		0.4675	0.2109	0.0693	0.0211
5491	8538.014	FeI			0.0442	0.2153	0.0213	0.0177
5515	8542.091	CaII	2	①⑥; a	0.2142	0.2200	0.0022	0.0096
5550	8548.098	TiI	150		0.2763	0.2238	0.0307	0.0215
5266	8499.606	FeII			0.0410	0.2262	0.0331	0.0157
5492	8538.175	FeI			0.0609	0.2362	0.0232	0.0191
6211	8661.898	FeI			0.4585	0.2476	0.0042	0.0166
5277	8501.544	SiI			0.3432	0.2609	0.1075	0.0182
5250	8496.984	FeI			0.0307	0.2647	0.0269	0.0192
5256	8498.023	CaII	2		0.1679	0.2918	0.0024	0.0122
5498	8539.127	FeI			0.0745	0.2956	0.0268	0.0211
5500	8539.468	TiI			0.1608	0.3420	0.0257	0.0245
5279	8501.799	NiI			0.4220	0.3637	0.1475	0.0234
6222	8663.716	FeI			0.0128	0.3826	0.0379	0.0230
5521	8543.151	SiI			0.1309	0.4149	0.0083	0.0205
5525	8543.734	CrI			0.0602	0.4799	0.0332	0.0254
5846	8598.825	FeI	1153		0.4076	0.4968	0.1187	0.0299
5842	8598.191	TiI			1.0413	0.5302	0.2349	0.0393
5281	8502.219	SiI			0.5009	0.5386	0.1755	0.0296
6230	8665.022	HI	9 (P13)		0.6274	0.5752	0.1553	0.0370
5844	8598.396	HI	9 (P14)	①; a	1.0008	0.6333	0.2313	0.0402
5534	8545.387	HI	10 (P15)	①; a	0.2521	0.7051	0.1916	0.0372
5284	8502.668	FeI			0.3806	0.7968	0.1566	0.0389
5283	8502.487	HI	10 (P16)		0.3754	0.8509	0.1569	0.0394

**RESULTS**  
from ANOVA  
for  $\log g$

Lines arranged  
in order of  
sensitivity to  $\log g$   
(B coefficient).

The most sensitive  
lines are Paschen lines,  
FeI and SiI.

## RESULTS FROM ANOVA

We identified the most sensitive lines to  $T_{\text{eff}}$  and  $\log g$ ...



But

Line depth is directly connected to the physical parameters only if the line is optically thin, not for core-saturated lines.

Synthetic spectra can not match the cosmic spread (nature has much more imagination than synthetic spectra!).

Synthetic spectra of cooler, larger stars differ from observed spectra.



II.  
GAIA WAVELENGTH RANGE  
8500-8750 Å

*OBSERVED SPECTRA*

*To identify directly diagnostic line ratios we analyzed the behaviour of the lines in the observed spectra.*

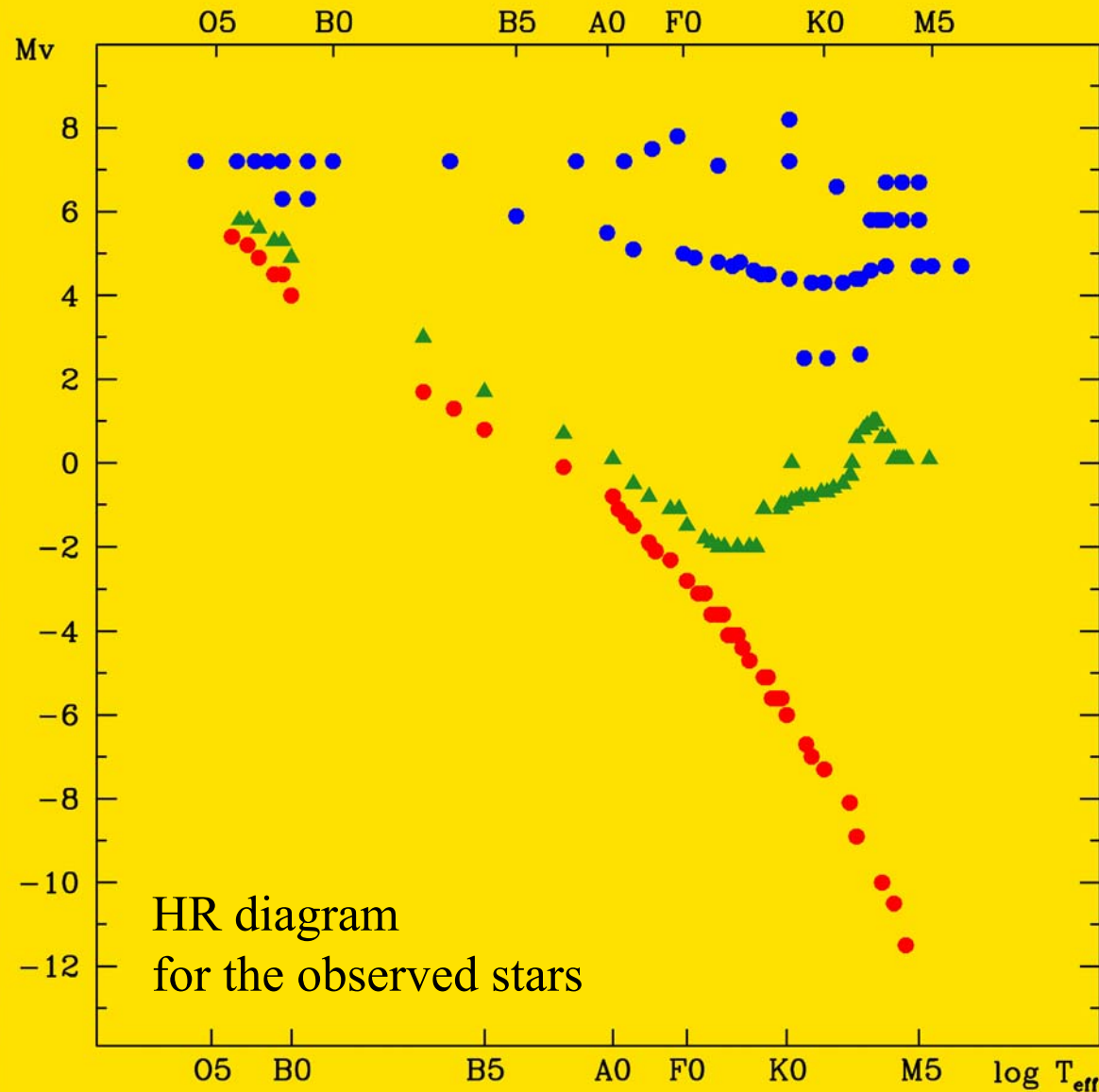
OBSERVED SPECTRA

to take into account the real conditions of the stars.

EQUIVALENT WIDTHS

are more correlated with the physical parameters.

# MK STANDARD STARS

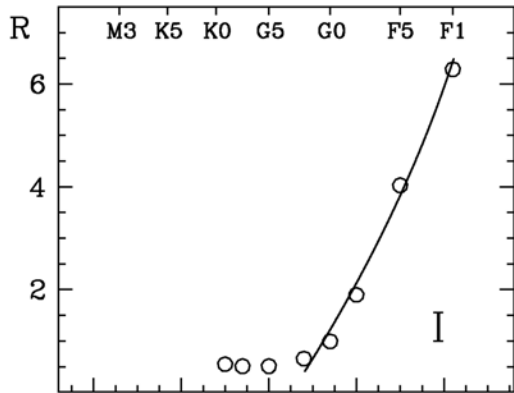


We needed a great deal of standard stars observed at resolutions similar to that of the GAIA spectrograph.

222 MK standard stars with the 1.82m of Cima Ekar (Asiago).

Munari & Tomasella,  
1999 *A&AS*, 137, 521  
Marrese et al. 2003  
*A&A*, 406, 995

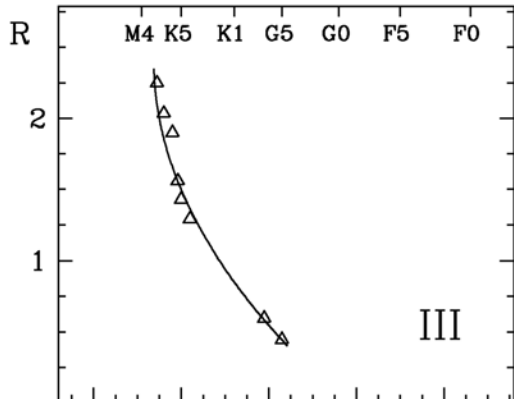




$$R = \frac{\text{Blend 8680}}{\text{FeI 8675}}$$

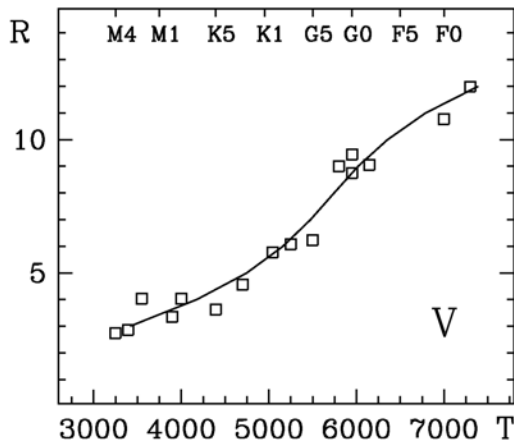
→ FeI 8679.6

$$T = 5257.3 + 380.1 R - 14.6 R^2$$



$$R = \frac{\text{TiI 8683}}{\text{Blend 8680}}$$

$$T = 5883.6 - 1826.3 R + 379.6 R^2$$



$$R = \frac{\text{CaII 8542}}{\text{FeI 8688}}$$

$$T = -607.8 + 1876.0 R - 204.0 R^2 + 8.6 R^3$$

## RESULTS FROM OBSERVED SPECTRA for $T_{\text{eff}}$

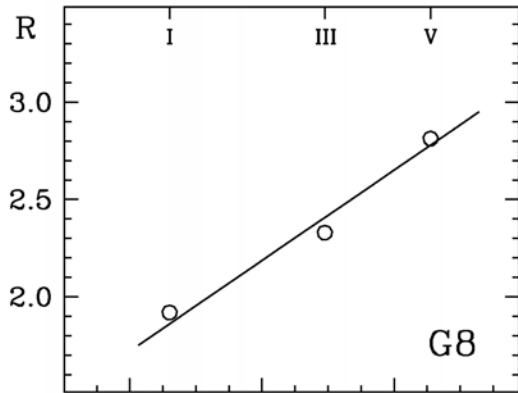
Simple numerical relations between R (ratio of EWs) and  $T_{\text{eff}}$ .

No/Yes metallicity depend.

GAIA resolution is appropriate

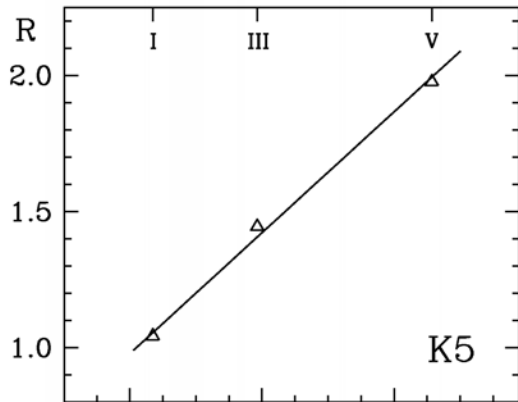
Simulation with blind test gives temperature with error: 70÷200 K.

From Boschi et al. 2003, PASP 303, 535



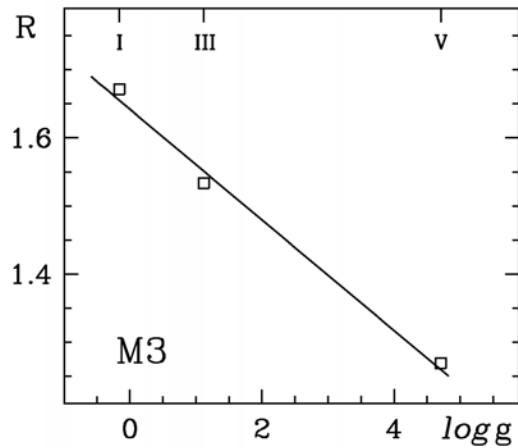
$$R = \frac{\text{FeI } 8688}{\text{FeI } 8675}$$

$$\log g = -7.4 + 4.3 R$$



$$R = \frac{\text{TiI} + \text{MgI } 8735}{\text{SiI} + \text{FeI } 8728}$$

$$\log g = -4.4 + 4.5 R$$



$$R = \frac{\text{FeI } 8514}{\text{TiI } 8518}$$

$$\log g = 20.2 - 12.3 R$$

## RESULTS FROM OBSERVED SPECTRA for log g

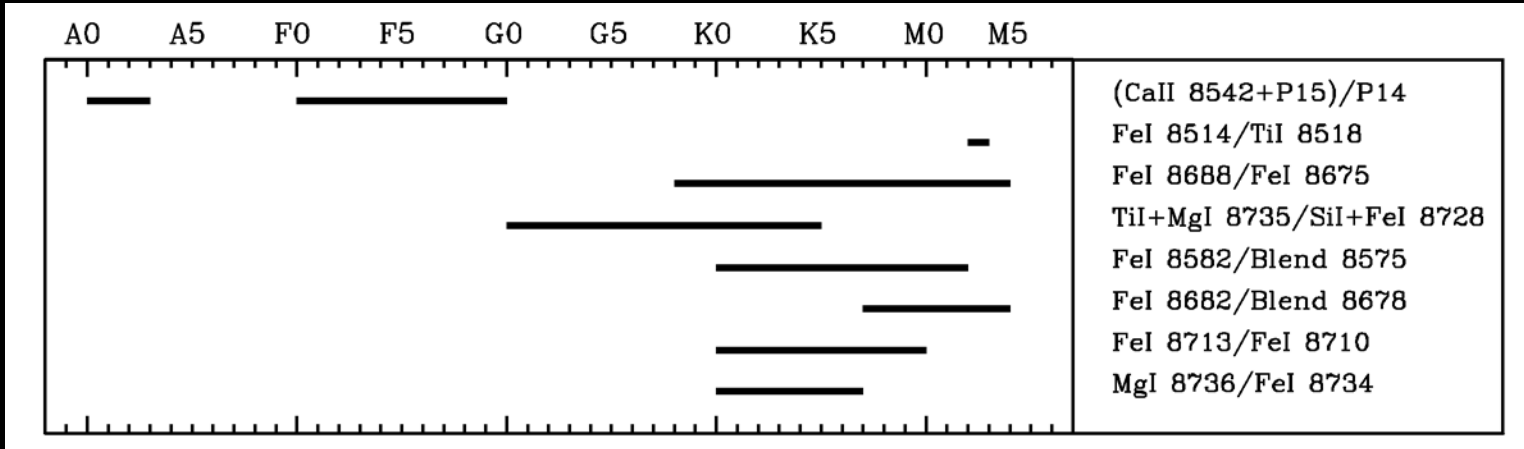
Simple Numerical relations  
between  
R (EWs ratio and log g ).

From Boschi et al.  
2003, PASP 303, 535

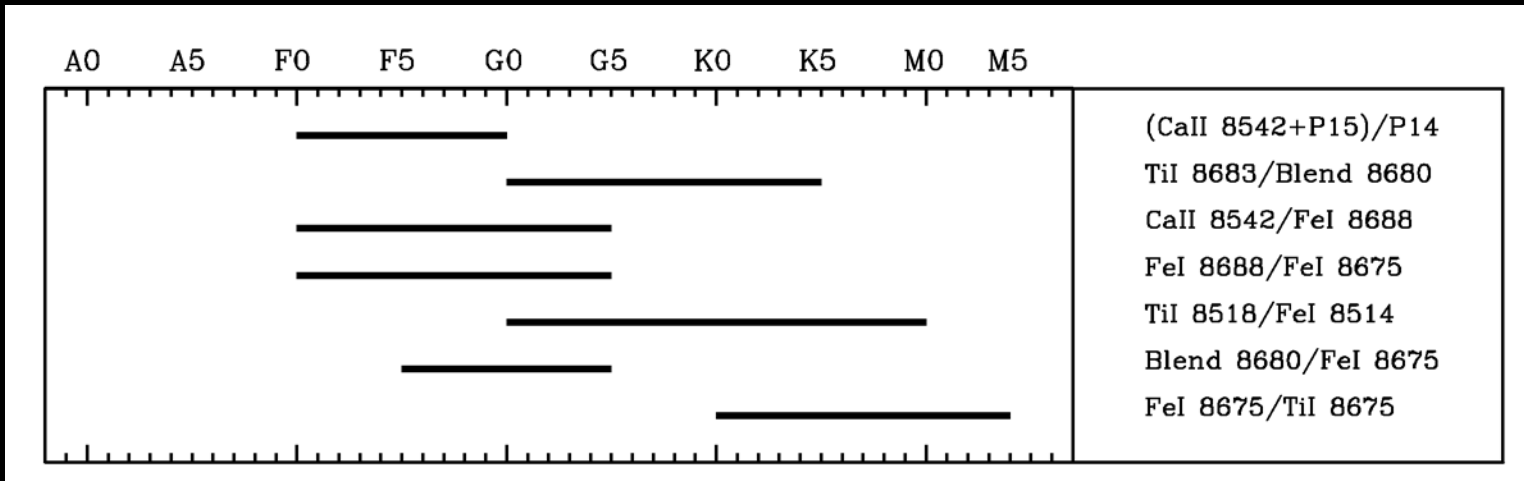
# RANGES OF VALIDITY

## Temperature

From very small to good ranges. Overlap. Cover entire range.



## Luminosity



# Summary

Possible line ratios for temperature:

22 relations for supergiants;

14 for giants;

9 for main sequence stars.

Possible line ratios for  $\log g$ :

identified some line ratios  
work in progress.

## Diagnostic lines ratios are useful tools:

- To derime cases in which photometry and Kurucz analysis are in disagreement (binary stars in which the companion is undetectable).
- To increase the velocity of the automatic analysis of spectra via Kurucz model (previous information about T and log g).



THE END

A fractal image with a blue background. The fractal is a complex, self-similar pattern that resembles a stylized eye or a flower. It is composed of many small, repeating shapes that form a larger, more intricate structure. The fractal is centered on the page. In the center of the fractal, there is a large black circle. Inside this circle, the words "THE END" are written in a white, serif font. The text is centered within the circle and is the most prominent feature of the image.

THE END