

# Stellar rotation and the age of star determination

## Application to stellar clusters

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# Overview

1. Introduction
2. Projected rotational velocity distribution:  
application to 5 open clusters
3. Confrontation theory and observation  
in the special case of Hyades  
→ AGE DETERMINATION
4. Conclusions and perspectives

# 1. Introduction

- Stellar physics in the Gaia context
- FLAME workpackage in CU8  
(Final Luminosity Age Mass Estimation)
- Test of rotation on stellar clusters
- Stellar structure and evolution with rotation

# 1. Introduction

## Why rotation is important?

- Rotation has an impact on the age determination (Maeder 1998, Chiosi 2009)
- To study **angular momentum**:
  - Loss of angular momentum from protostellar cloud to MS stars; (see Maeder 2009)

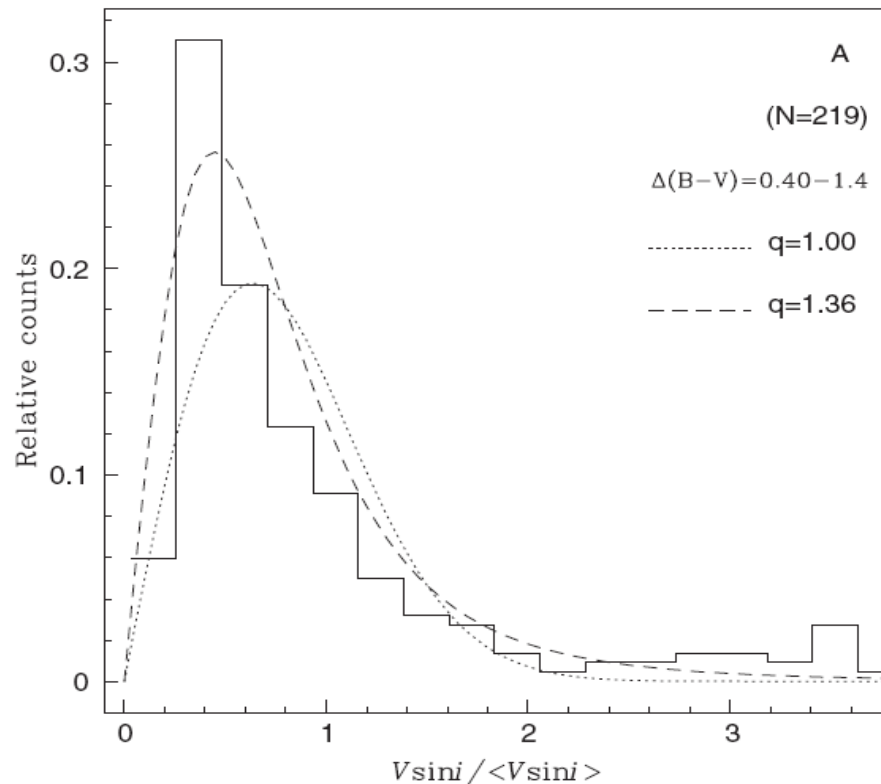
The observed specific angular momentum in various objects ( $\text{cm}^2 \text{s}^{-1}$ )

Dense molecular cores	$10^{21-22}$
Wide binaries	$10^{19-20}$
Pre-MS stars (TTauri)	$10^{16-17}$
Sun	$10^{15}$

- Scenario: magnetic field – angular momentum loss (Schatzman 1962)

# 2. Rotational velocity distribution

Pleiades (Soares et al. 2006)



obs. Vrot      true Vrot      inclination

$$y = x \cdot \sin i$$

Random distribution of  $i$   
 Integral relation; Gaussian form;  
 Maxwell-Boltzmann form  
 Polynomial form  
 Non gaussian

$$\phi_q(y) = B_q y \left[ 1 - (1 - q) \frac{y^2}{\sigma^2} \right]^{1/(1-q)}$$

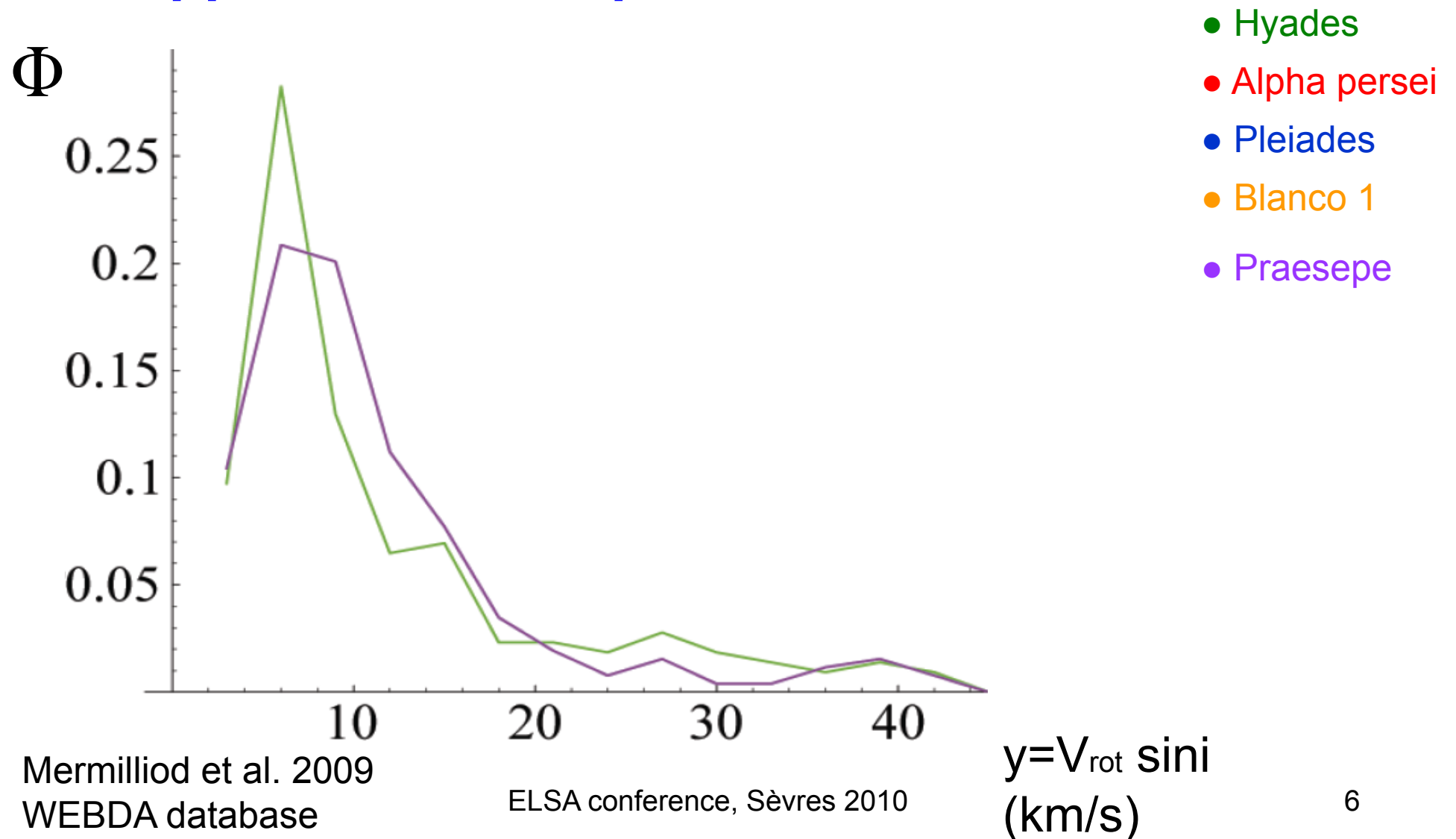
$$y_{peak} = \frac{\sigma}{\sqrt{3 - q}}$$

Shape parameter

Confirmation of random distribution of spin axes via Monte-Carlo simulation:  
 Jackson & Jeffries 2009 arXiv 0911.1075J

## 2. Rotational velocity distribution

### Application to 5 open clusters



## 2. Rotational velocity distribution

### Results of our statistical analysis

	Alpha Persei	Pleiades	Blanco 1	Hyades	Praesepe
q	1,14	1,38	1,51	1,51	1,54
$\sigma$	16,83	8,75	4,27	4,27	4,02
y <sub>peak</sub>	12,34	6,91	3,5	3,5	3,34
age (Myr) *	35	120	208	650	800

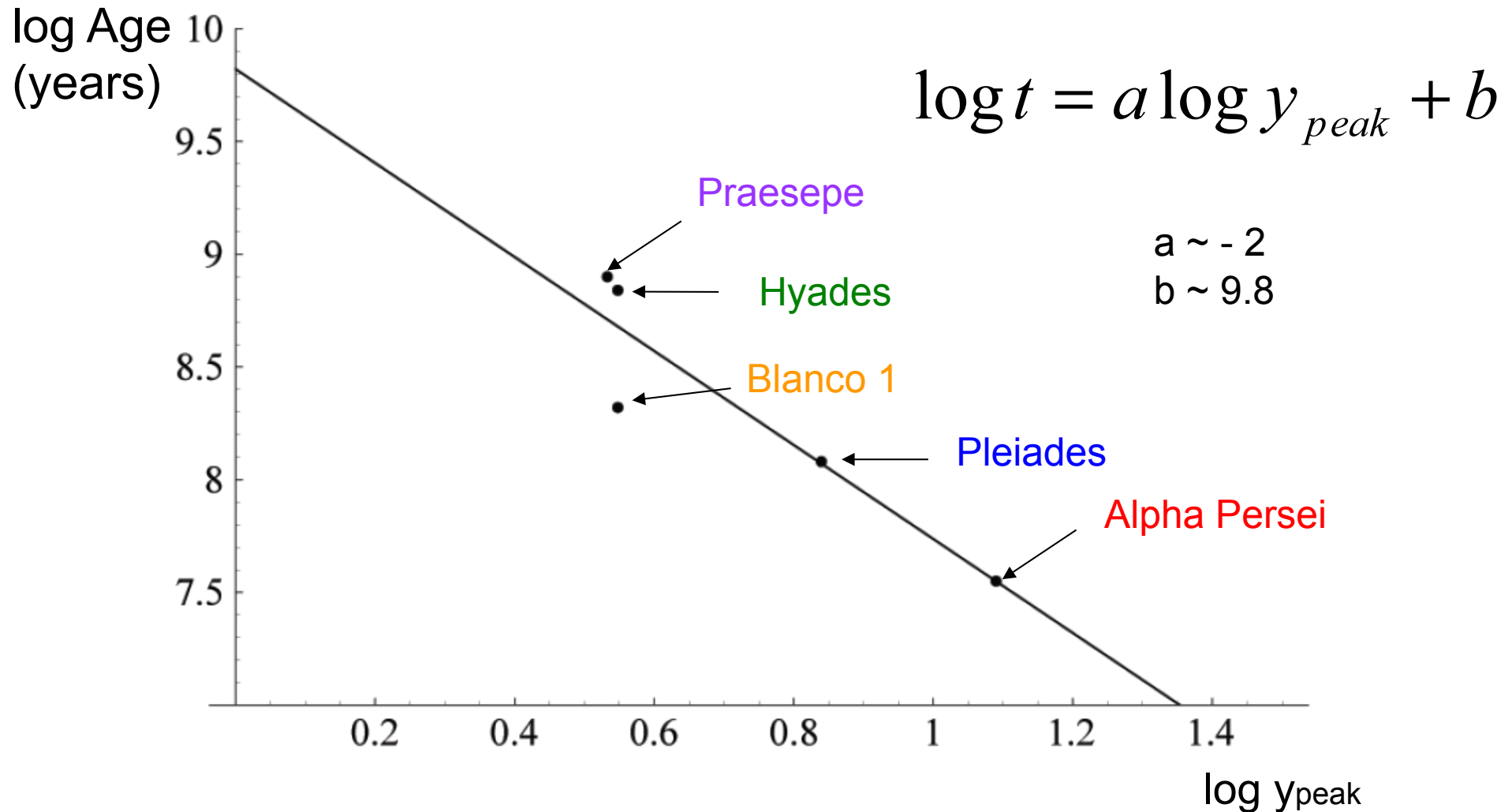
\* age from Van Leeuwen 2009,

Lebreton et al. 2001

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## 2. Rotational velocity distribution

### Determination of a deceleration law





# 3. Confrontation theory and observation in the special case of Hyades

- **Advantages**

- Distance, metallicity & helium abundance known with good accuracies
- Known  $V \sin i$
- Few known binary systems (masses,  $\sin i$ )

Perryman M. A. C. et al. 1998, Lebreton Y. et al. 2001, Cayrel de Strobel G. et al. 1997, Mermilliod J.-C. et al. 2009, WEBDA database, Patience J. et al. 1988

# 3. Confrontation theory and observation in the special case of Hyades

- **Stellar evolution code: Cesam2k (Morel 1997 & Pichon)**
  - Convection theory Canuto & Mazzitelli (1991)
  - MARCS atmospheres (Gustafsson et al. 2008)
  - Burgers diffusion
  - EOS OPAL Rogers & Iglesias (1992)
  - **no overshoot**
  - **Rotation theory: Maeder & Zahn (1998) and following papers**
    - We need  $V_{rot}$  for each star

### 3. Confrontation theory and observation in the special case of Hyades

#### Distribution of $V_{rot}$ (= $x$ ) from $V_{rot} \sin i$ (= $y$ )

- Using Soares et al 2006 function, we reproduce the observational distribution function
- We reconstruct the distribution  $f(x)$  of  $V_{rot}$  using Chandrasekhar & Munch (1950) inversion formula

$$f(x) = -\frac{2}{\pi} x^2 \frac{\partial}{\partial x} x \int_x^\infty \frac{\phi(y)}{y^2 (y^2 - x^2)^{1/2}} dy$$

### 3. Confrontation theory and observation in the special case of Hyades

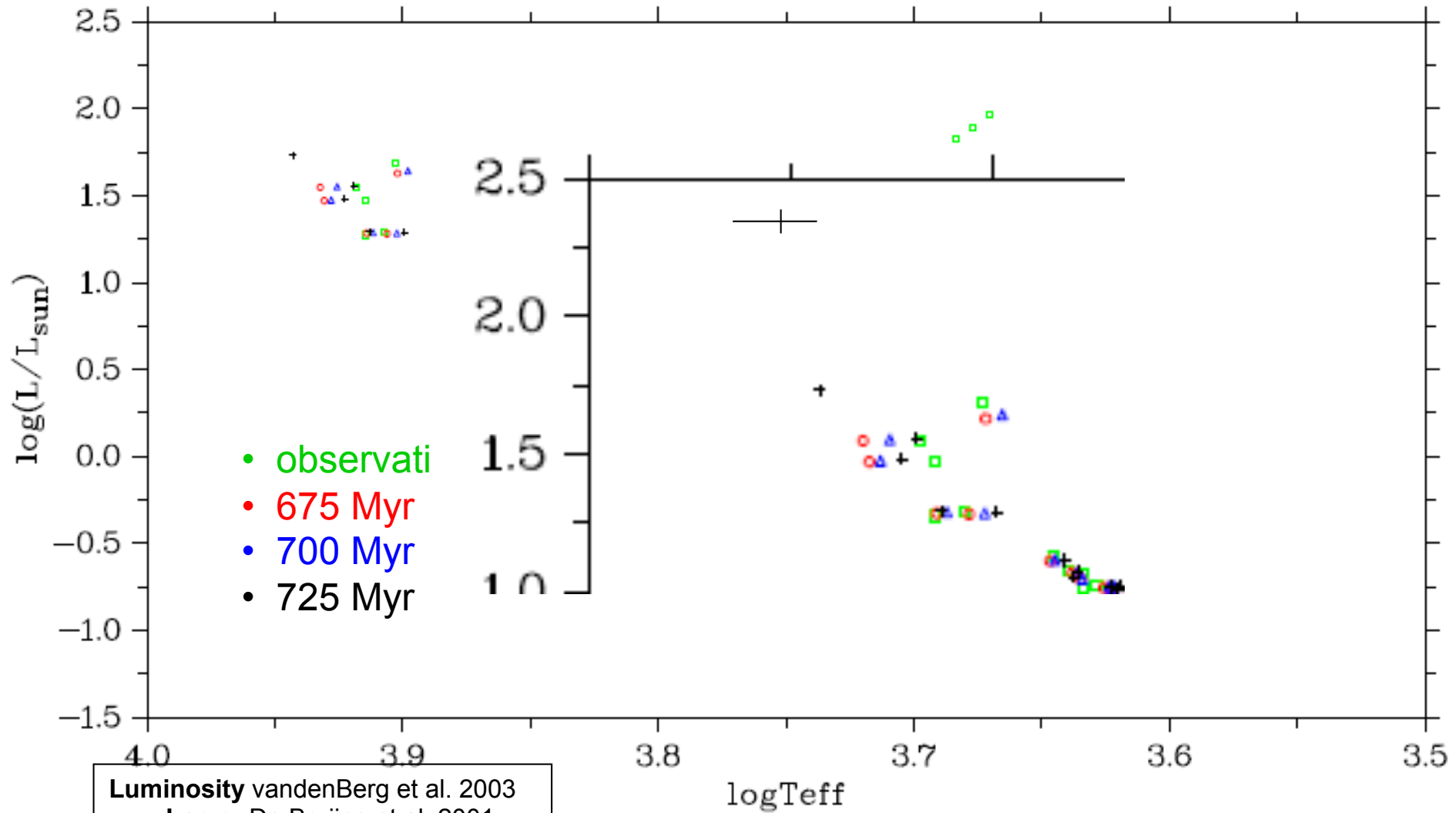
We tested our procedure on Hyades binary stars:

Name	<b>Vrot sin i (km/s)</b>	<b>Vrot (km/s)</b>	<b>Statistical Vrot (km/s)</b>
HIP 20019	$10.7 \pm 2.7$	$10.7 \pm 2.7$	$15 \pm 2$
HIP 20087	$100.8 \pm 5.0$	$123.2 \pm 6.2$	$129 \pm 2$
HIP 20894	$16.3 \pm 1.0$	$19.9 \pm 1.2$	$21 \pm 2$

Torres et al 1997 I, II, III  
Peterson & Solensky 1988

Our results 

# 3. Confrontation theory and observation in the special case of Hyades



**Luminosity** vandenBerg et al. 2003  
**Log g** De Bruijne et al. 2001  
**Log g** Beck 2008  
**Log Teff** Alonso et al. 1996

## 6. Application to Hyades

### Comparisons with different CESAM evolution models

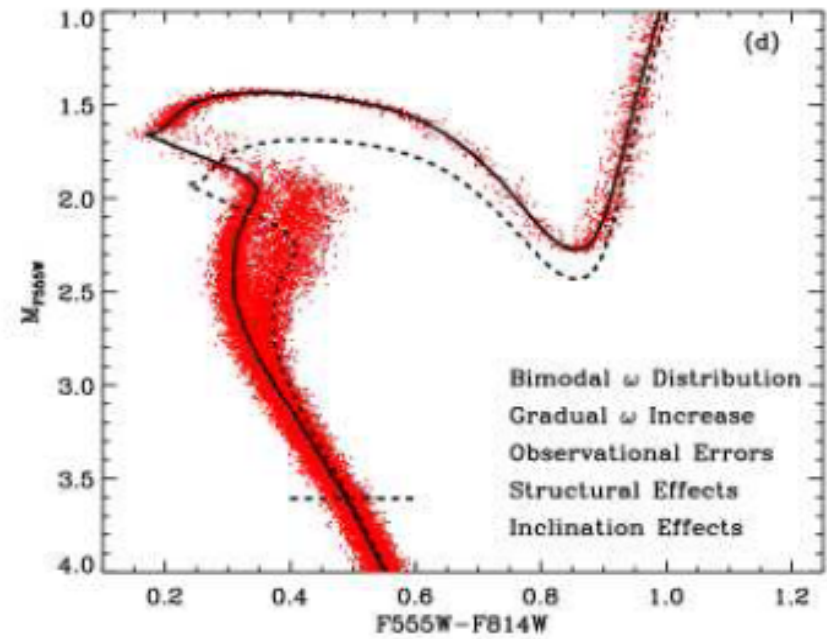
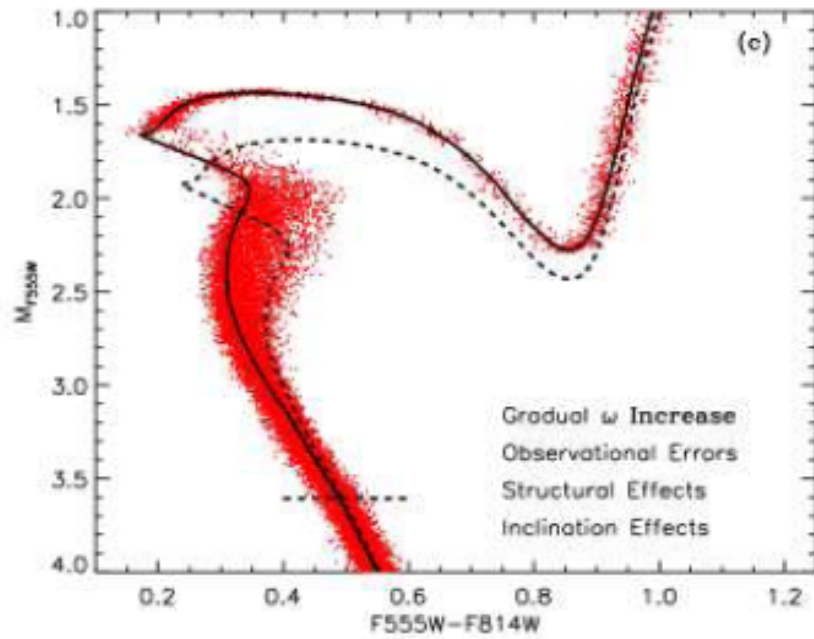
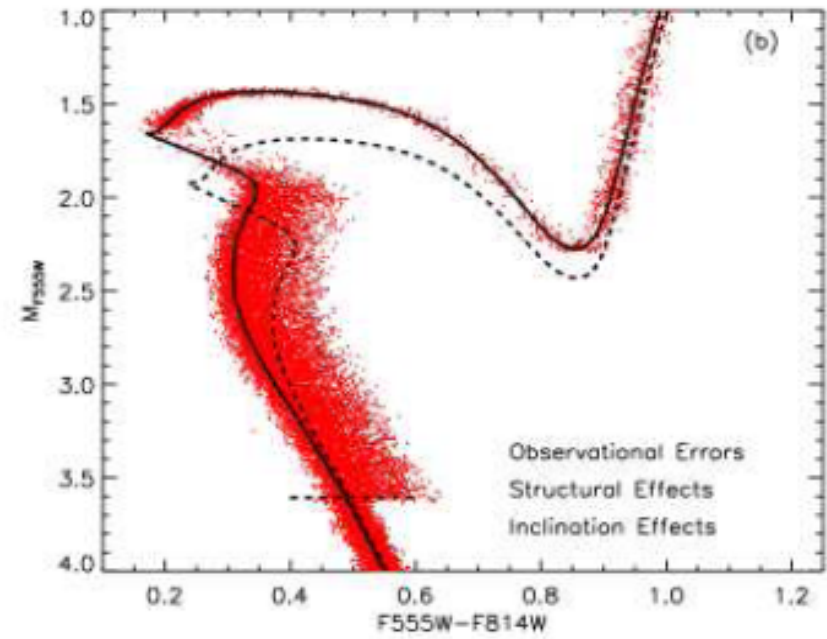
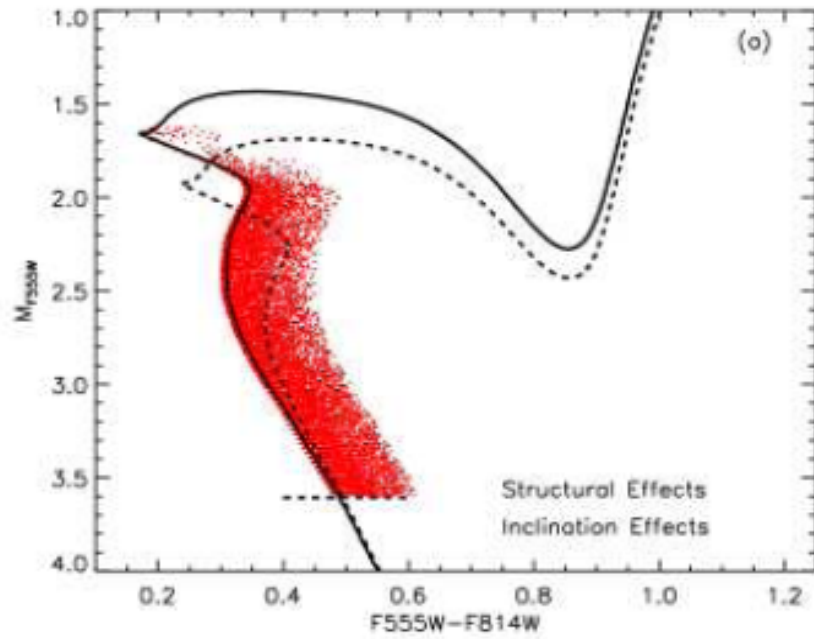
- Perryman et al. 1998:  $625 \pm 50$  Myr
- Lebreton et al. 2001: 650 Myr
- De Bruijne et al. 2001: 625 Myr
  
- Morel & Thévenin 2002:  $570 \pm 15$  Myr  
without rotation
- **Our age determination:  $700 \pm 25$  Myr**  
**with rotation**

# Conclusions / Perspectives

- Context Gaia data processing
- Statistical inversion
  - Vrot distribution law
- Stellar evolution with rotation
  - Age determination of Hyades cluster (15 % older)
- We need isochrones with rotation  
for ages < 1.5 Gyr for Gaia auxiliary data of DPAC
- Applications to multiple systems  
with masses > 1.5 Msun







Bastian, de Mink 2009

- Hyades
- Alpha persei
- Pleiades
- Blanco 1
- Praesepe

