

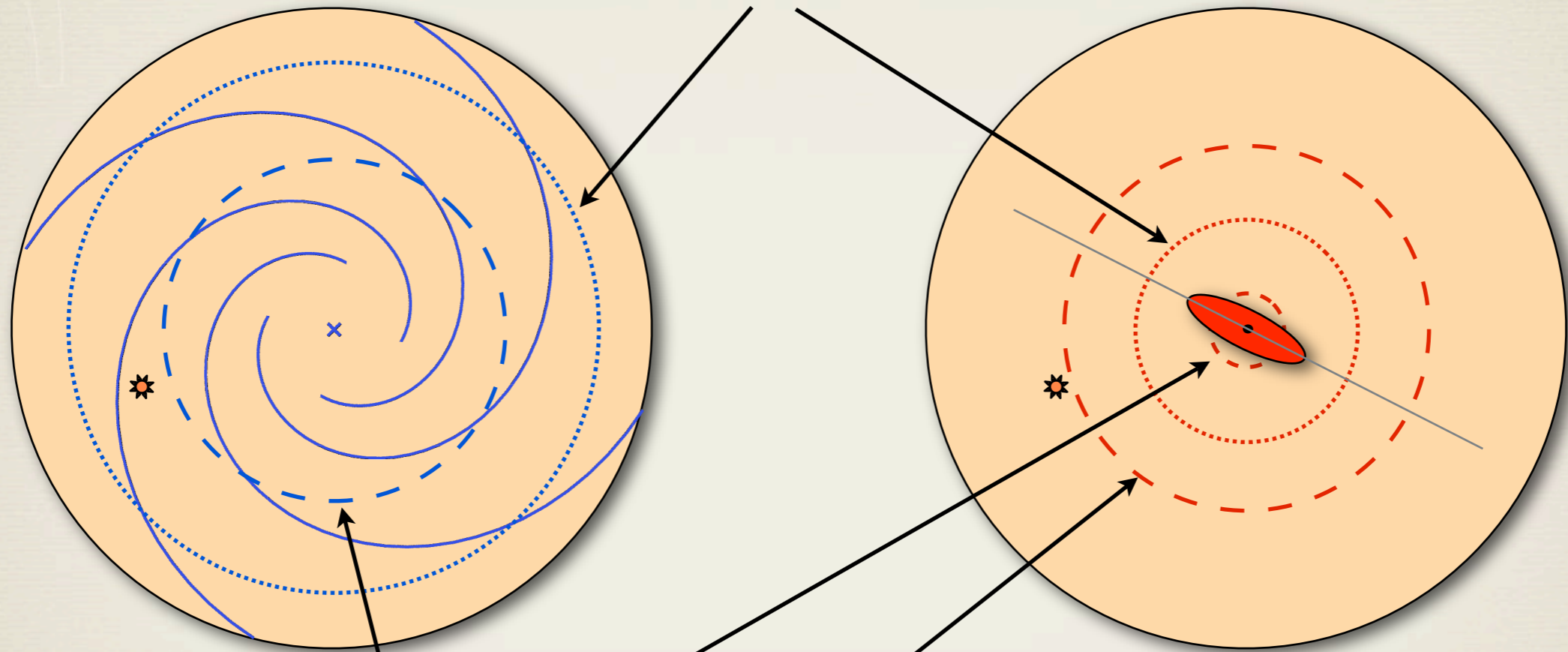
Radial mixing of galactic discs

Current mechanisms

- The metallicities of stars in the solar neighborhood lack the expected correlation with age ([Edvardsson et al. 1993](#); [Haywood 2008](#)).
- Explained by stellar radial migration in the disc:
 - ◆ Transient Spirals ([Sellwood & Binney 2002](#))
 - ◆ Small satellites can mix the outer disc ([Quillen, Minchev, Bland-Hawthorn & Haywood 2009](#))
- **Are galactic Bars important for Radial Migration?**

Resonances in galactic disks

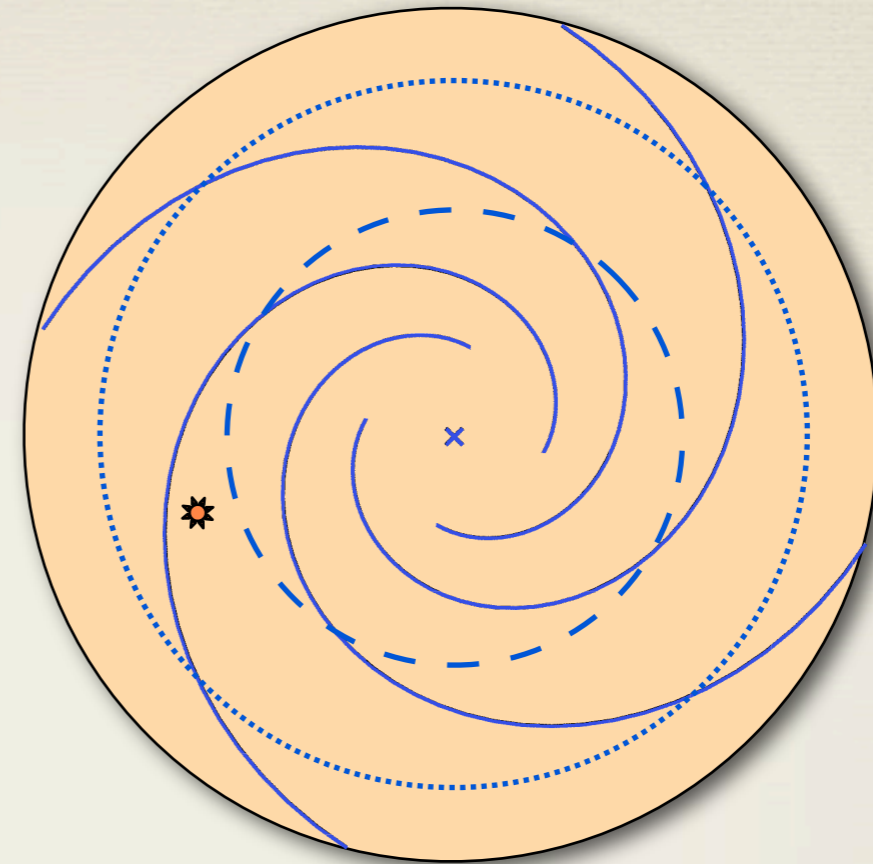
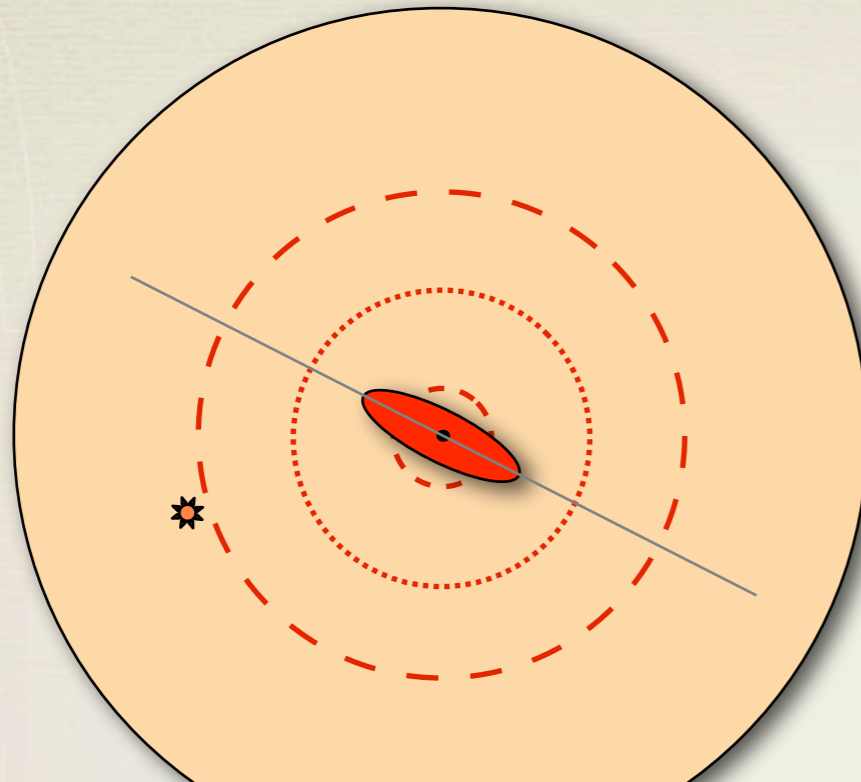
Corotation $\Omega_s = \Omega_0$



Inner and Outer Lindblad resonances

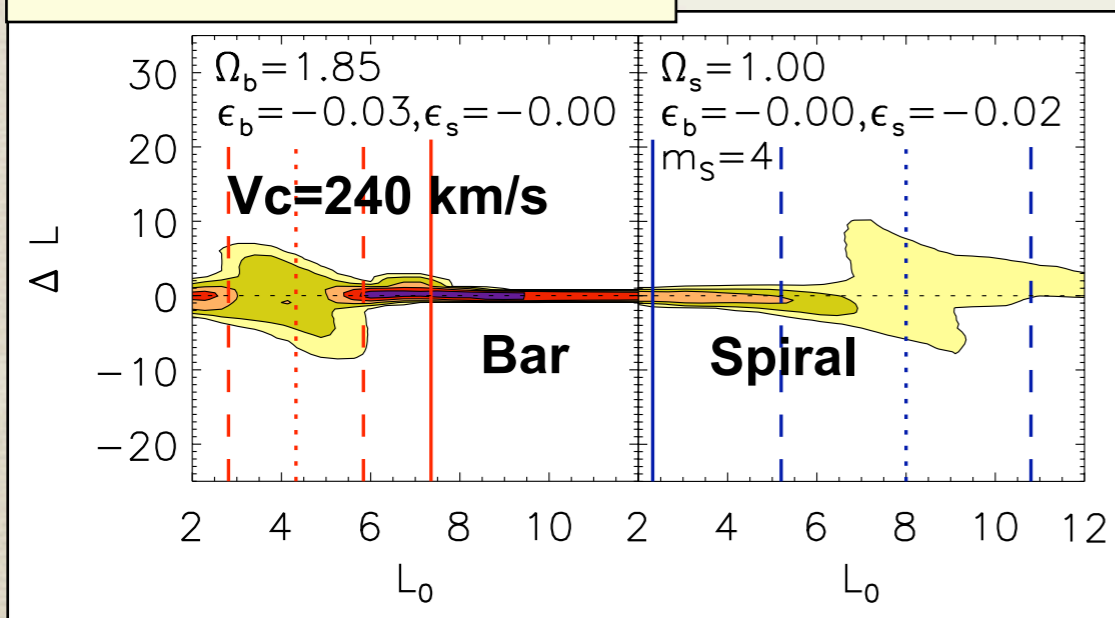
• For a flat rotation curve $\Omega_s = \Omega_0 \pm \kappa / m$

Radial migration due to a single perturber



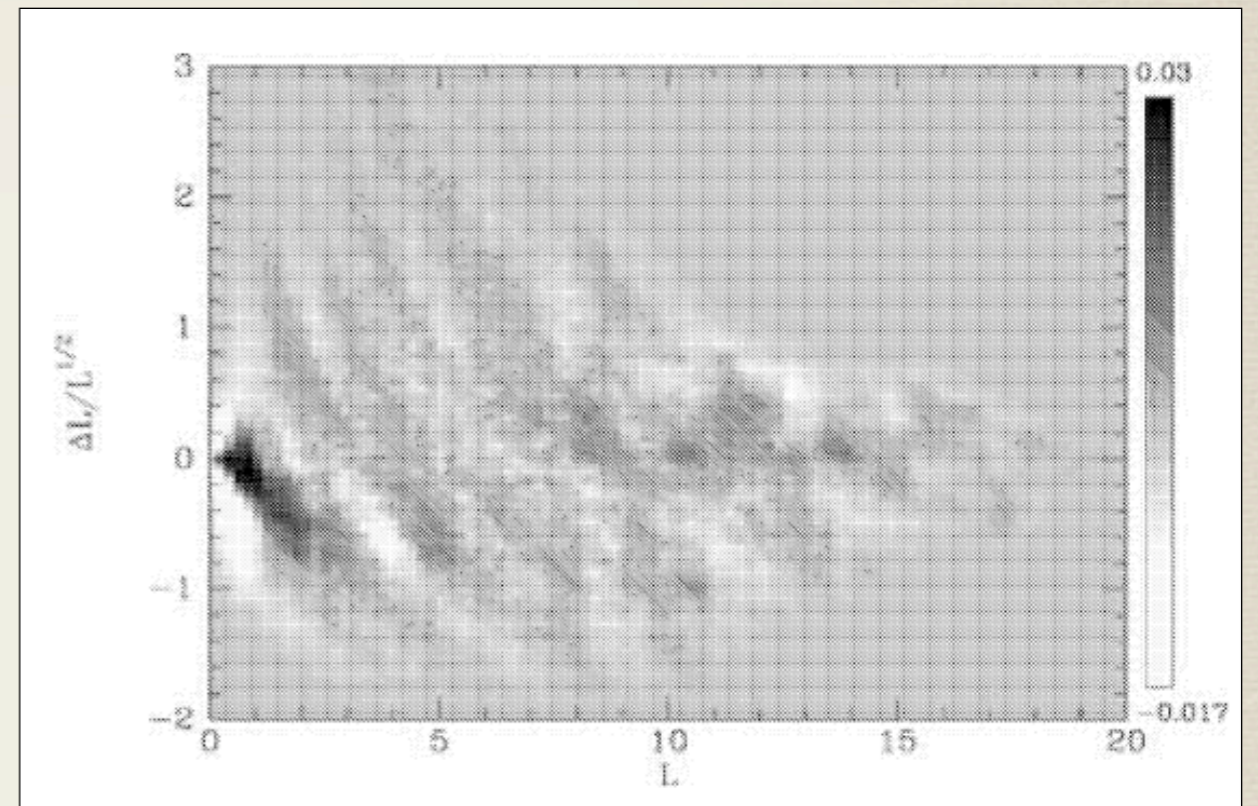
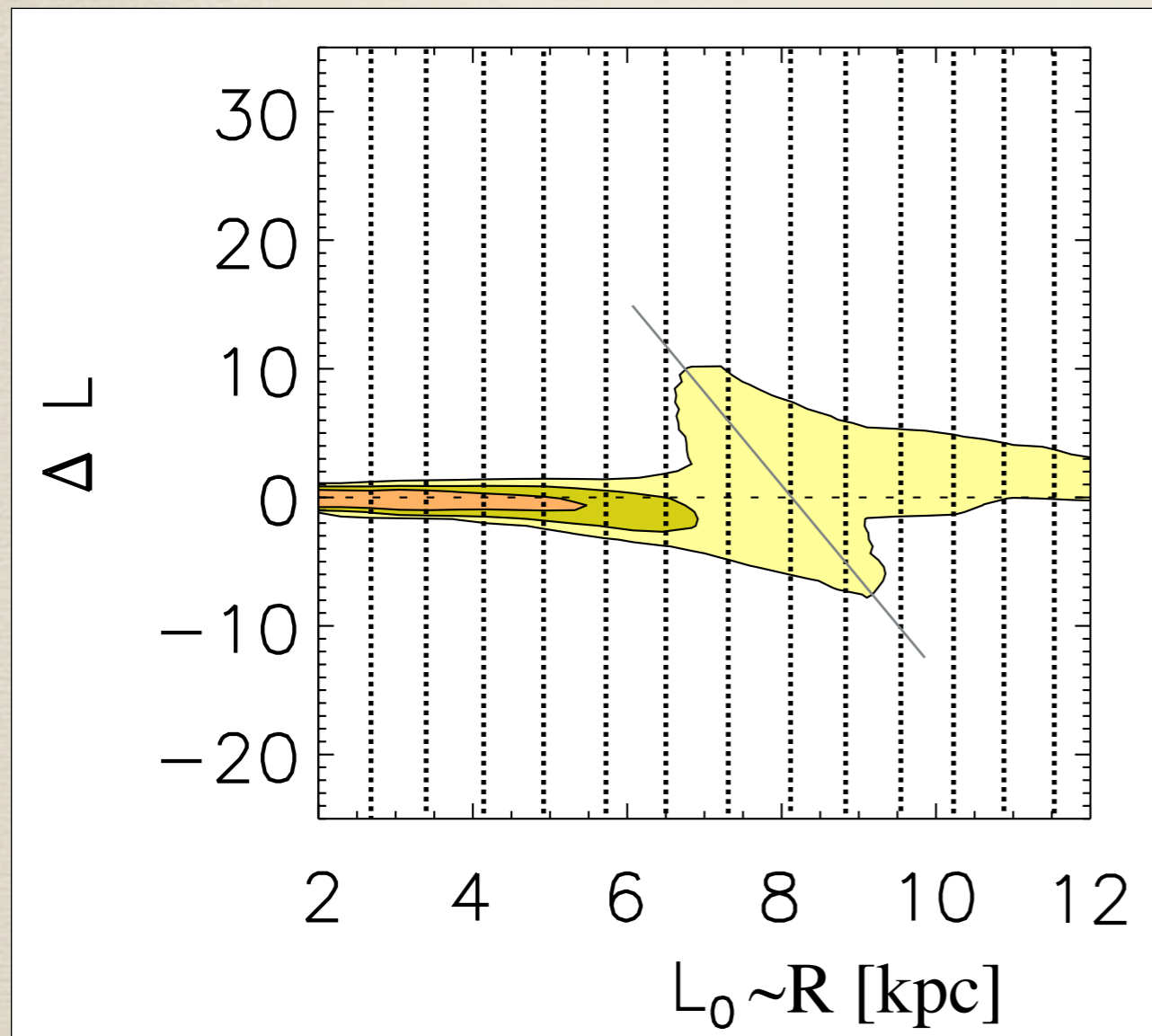
Change in angular momentum

No variation with time



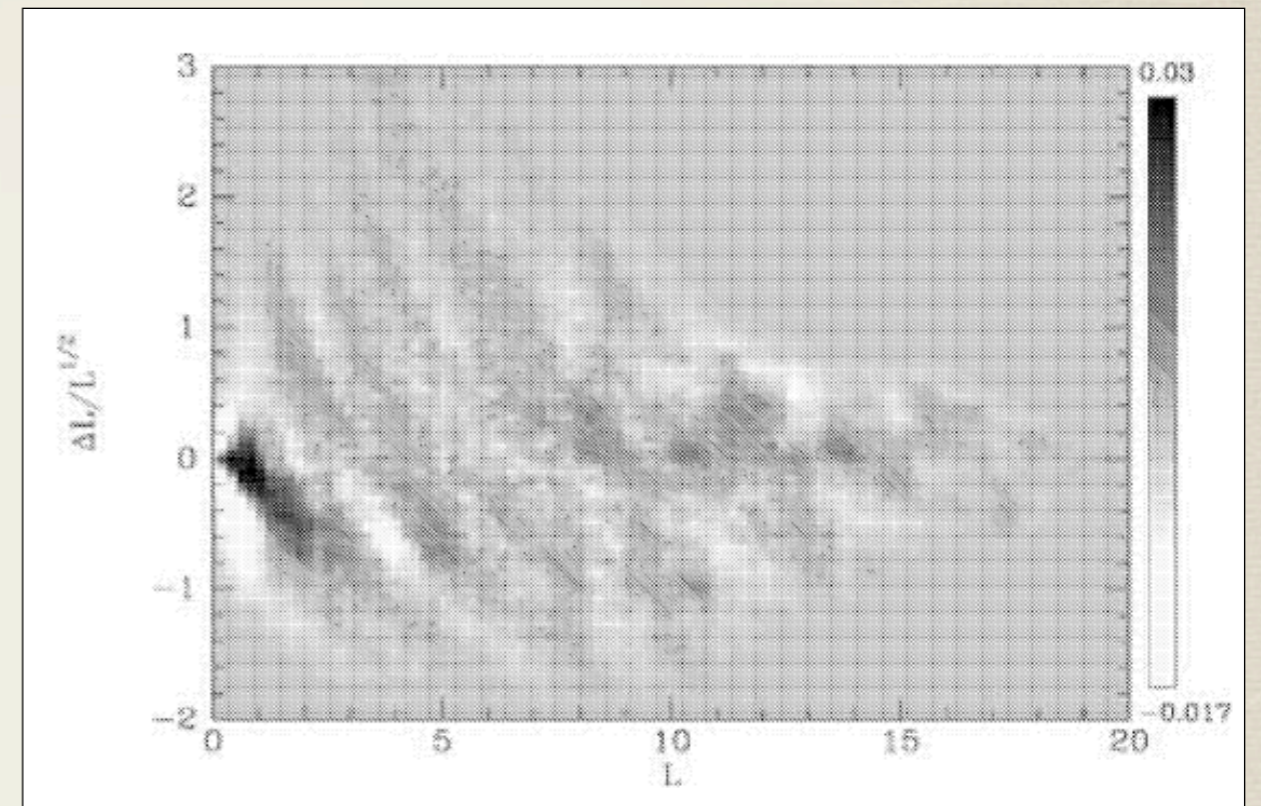
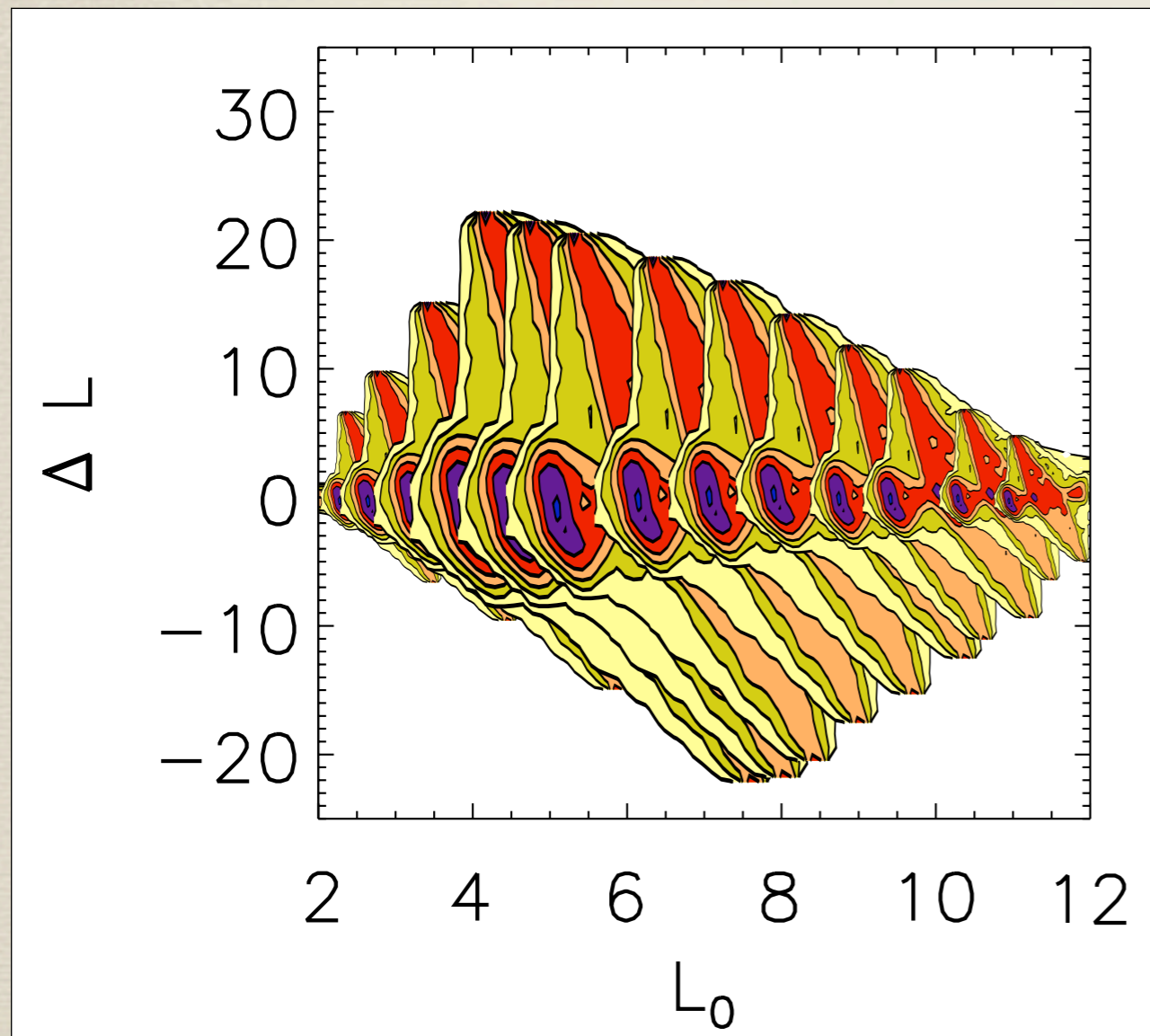
- Stars mix only near the corotation resonance of the **Bar** or **Spirals** (dotted lines).
- Not nearly enough to explain observations.

Radial migration from Transient Spirals



Sellwood & Binney (2002)

Radial migration from Transient Spirals



Sellwood & Binney (2002)

Requires ~ 9 Gyr for sufficient mixing

Hamiltonian including two perturbations

Third-order, post-epicyclic approximation

$$H_0(I_1, \theta_1; I_2, \theta_2) = aI_1^2 + 2bI_1I_2 + cI_2^2 + \kappa I_1 + \Omega I_2 + \dots \quad \text{Contopoulos (1975, 1988)}$$

$$H(I_1, \theta_1; I_2, \theta_2) \approx H_0 +$$

$$\epsilon_b I_1^{1/2} \cos[\theta_1 + 2(\theta_2 - \Omega_b t)] +$$

Perturbation from Bar

$$\epsilon_s I_1^{1/2} \cos[\theta_1 - m(\theta_2 - \Omega_s t) - \gamma]$$

Perturbation from Spiral

After a canonical transformation with a resonant angle $\phi = \theta_1 \pm m(\theta_2 - \Omega_p t)$

$$H(J_1, \phi) \approx aJ_1^2 + \delta J_1 + \beta J_1^{1/2} \cos(\phi) + \epsilon J_1^{1/2} \cos(\phi + \nu t - \gamma)$$

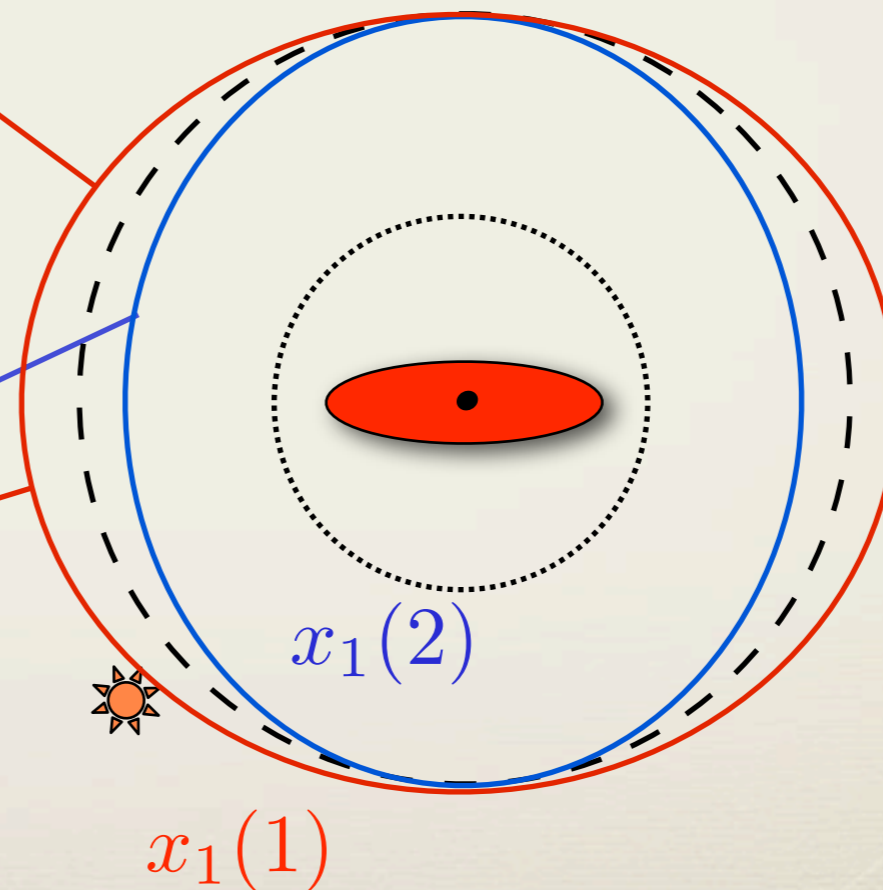
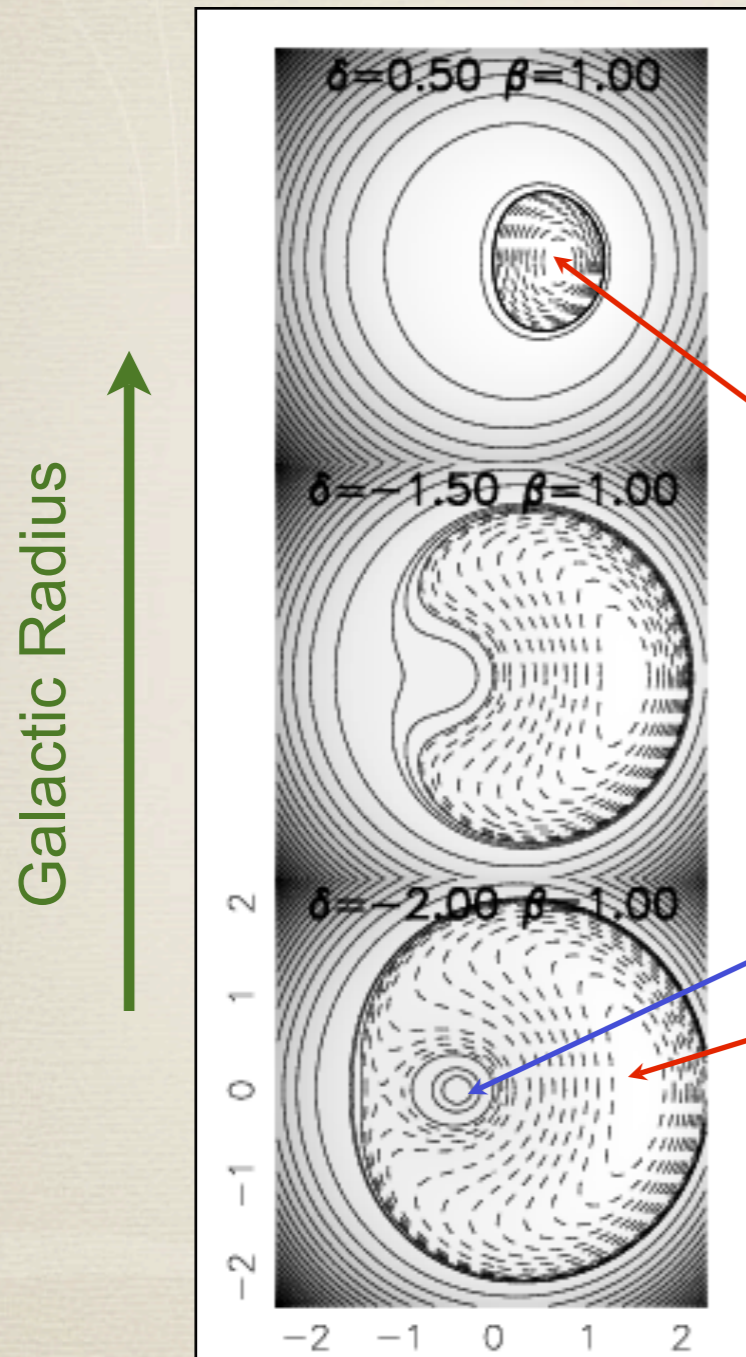
This is time independent and J_2 is conserved

First order Lindblad Resonances with the Bar

Hamiltonian description

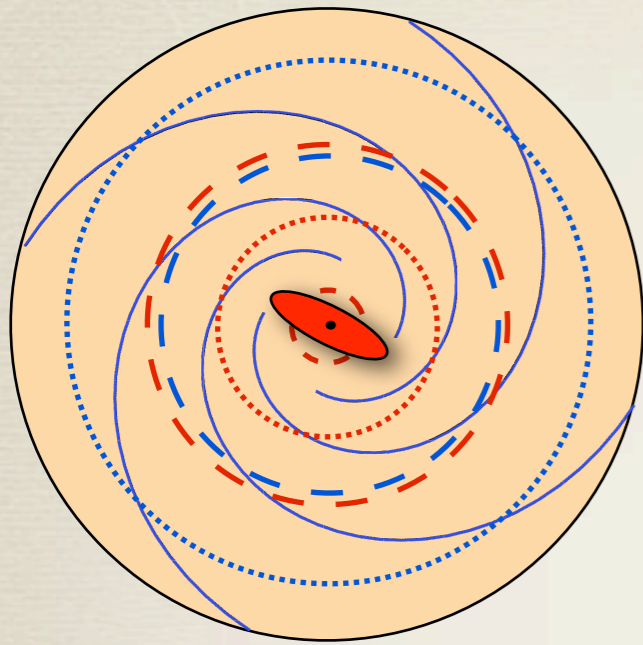
$$H(J_1, \phi) \approx aJ_1^2 + \delta J_1 + \beta J_1^{1/2} \cos(\phi)$$

$R = 2J_1$ Radius related to eccentricity



Closed orbits correspond to fixed points

Hamiltonian including two perturbations: Analogy to the forced pendulum



Strength of first
perturbation

Strength of second
perturbation

$$H(J_1, \phi) \approx aJ_1^2 + \delta J_1 + \beta J_1^{1/2} \cos(\phi) + \epsilon J_1^{1/2} \cos(\phi + \nu t - \gamma)$$

Controls center of first
resonance and depends
on radius

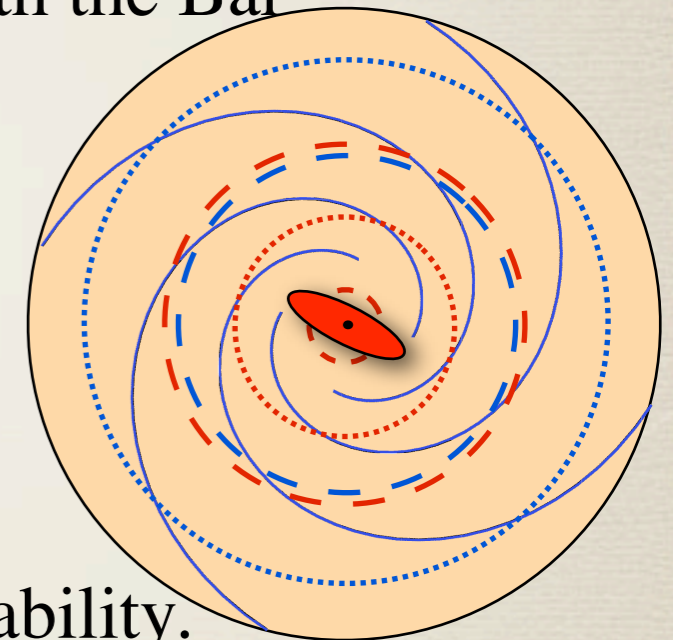
Controls spacing between
resonances and also depends
on radius

Spiral structure at the Bar's Outer Lindblad Resonance

- Oscillating primarily with spiral structure
- Perpendicular to Spiral Structure
- Oscillating primarily with the Bar
- Perpendicular to the bar

Area-filling orbits

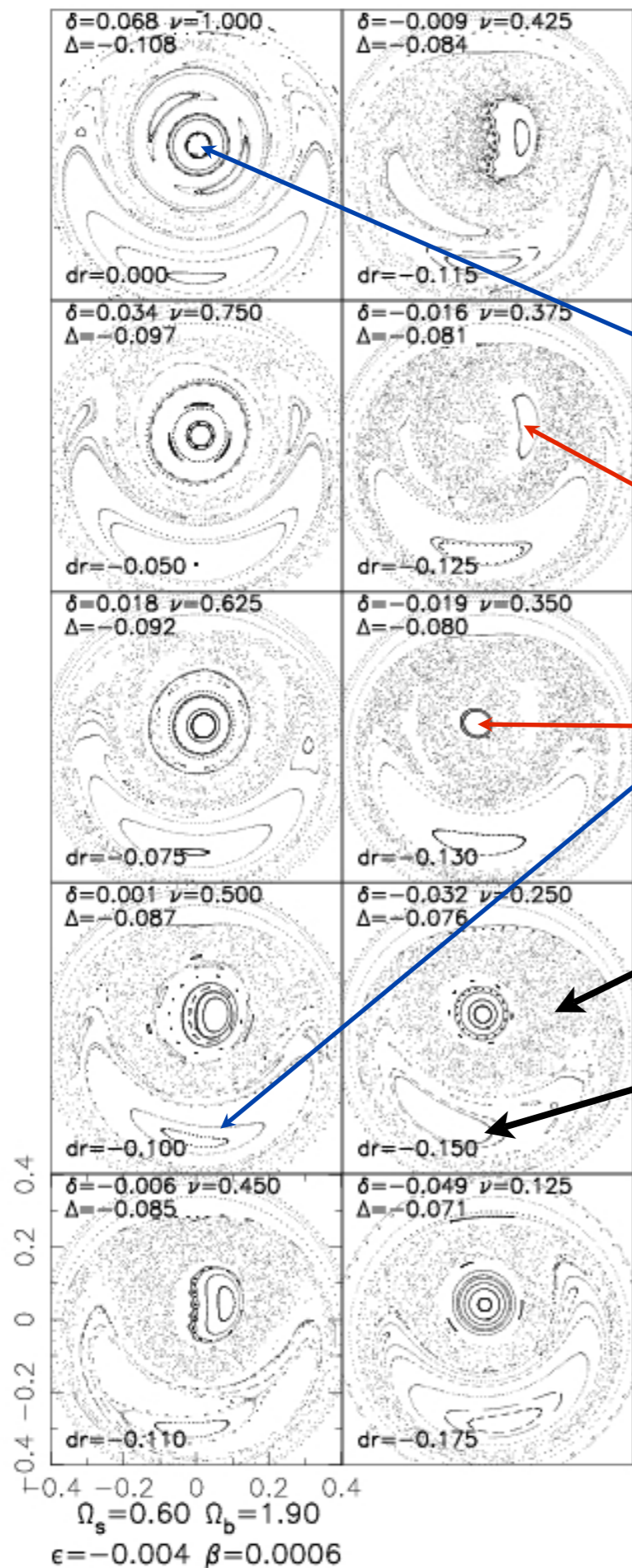
Quasi-periodic orbits



Poincare maps used to look at stability.

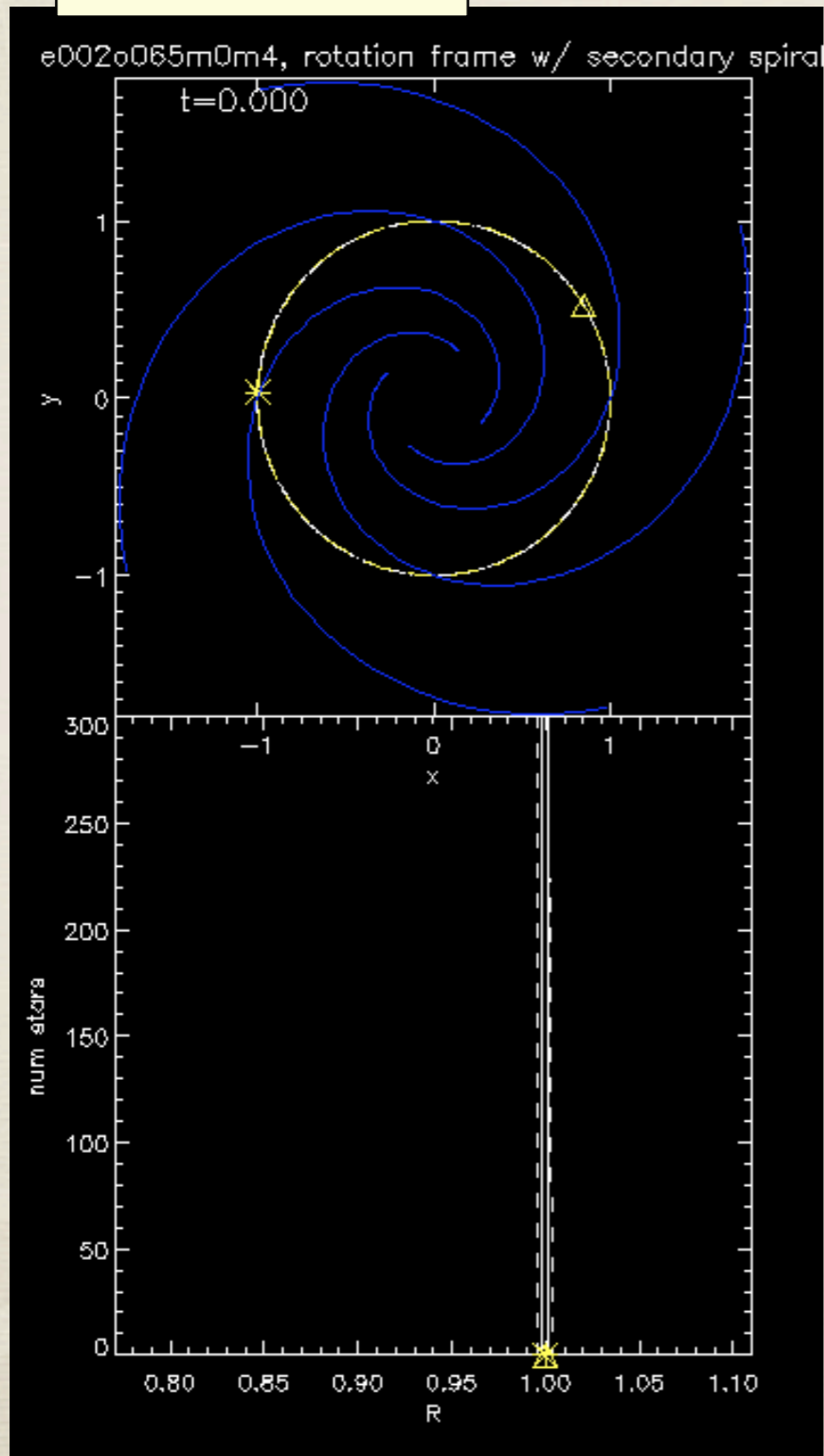
Plot every $\Delta t = \frac{2\pi}{\nu}$

Orbits are either oscillating with both perturbations or are **Chaotic**: Induces **Heating** and **Migration** (Quillen 2003)

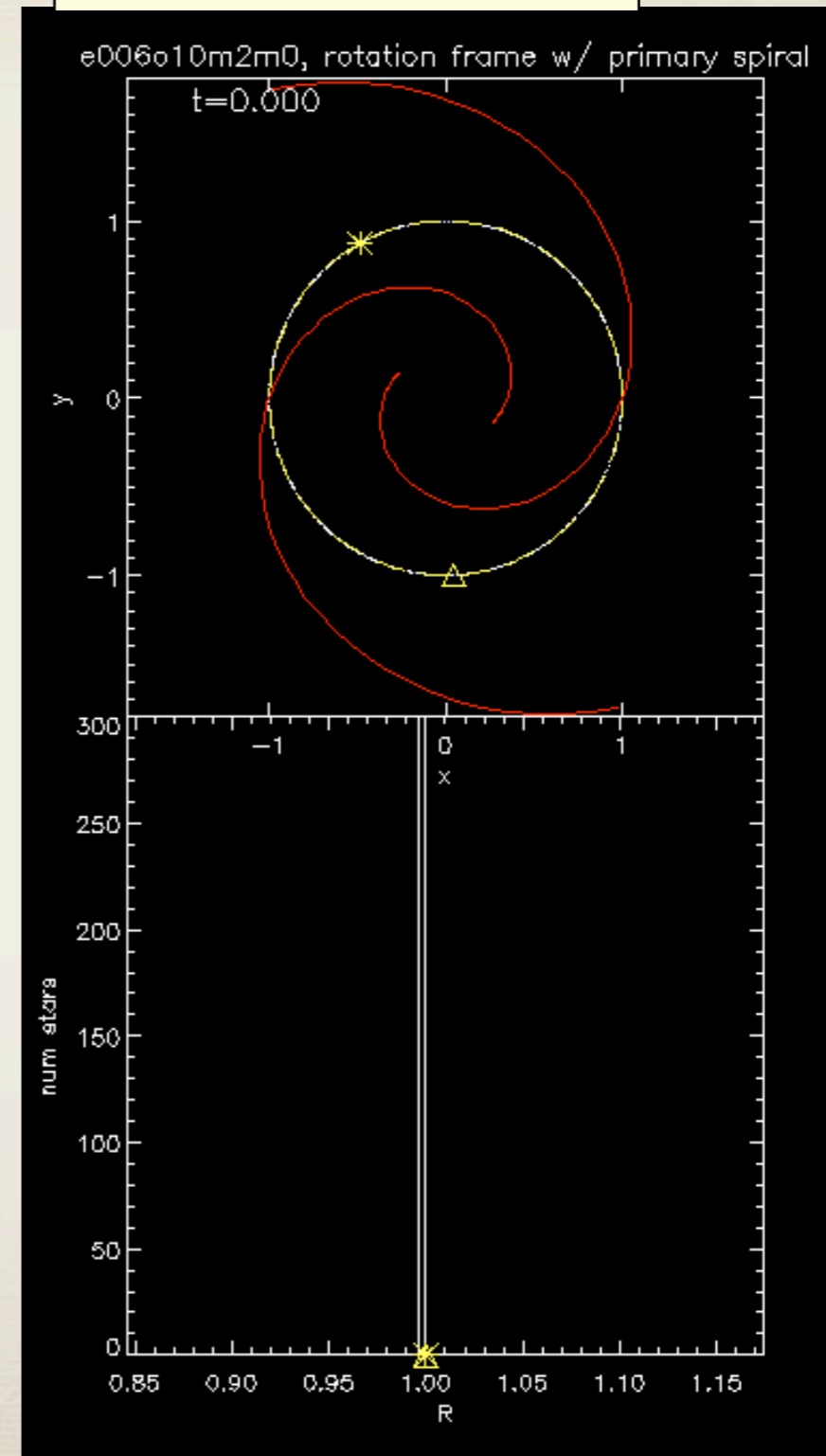


Radial migration at Corotation with Spiral

$m=4$ at OLR



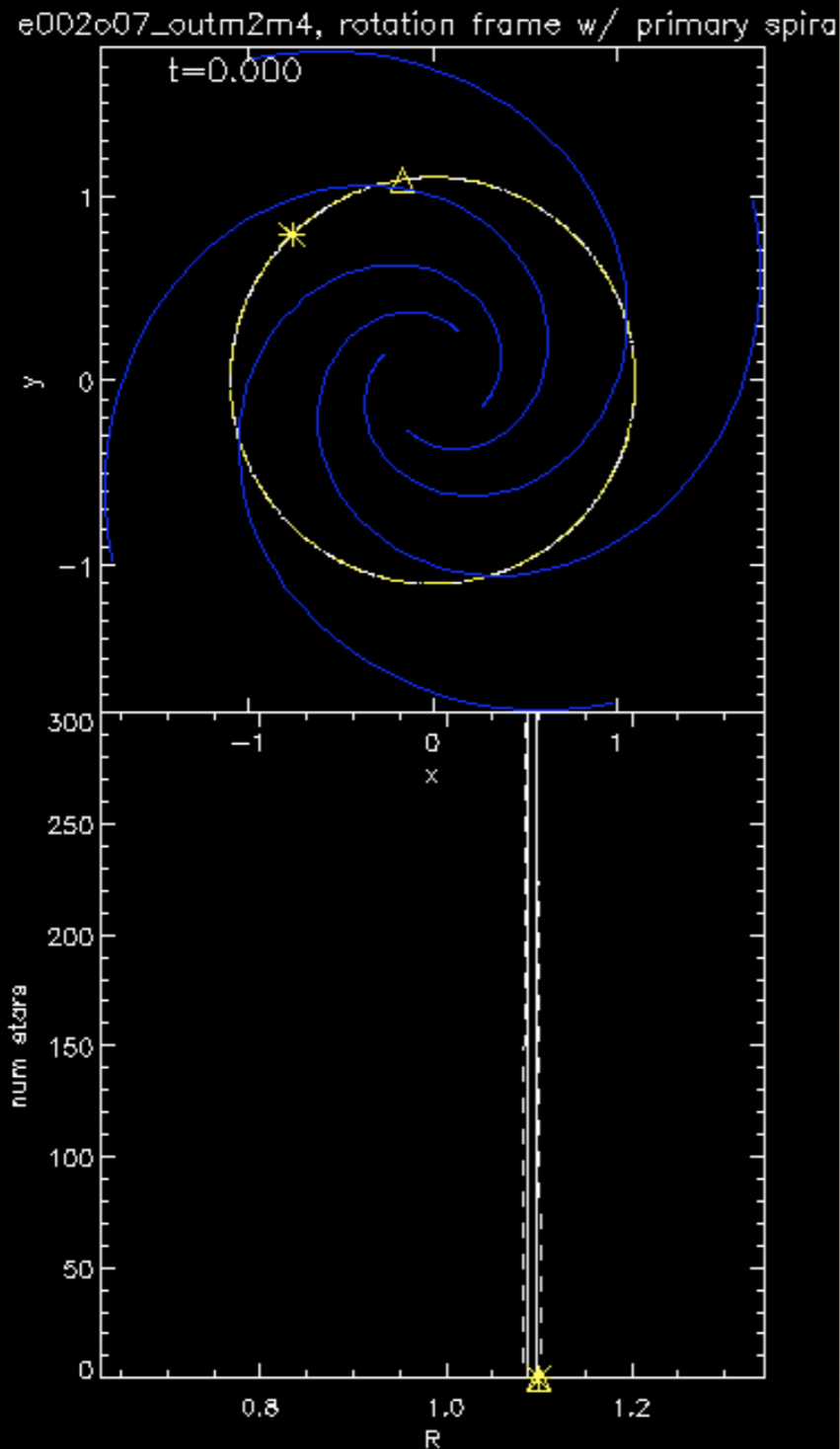
$m=2$ at Corotation



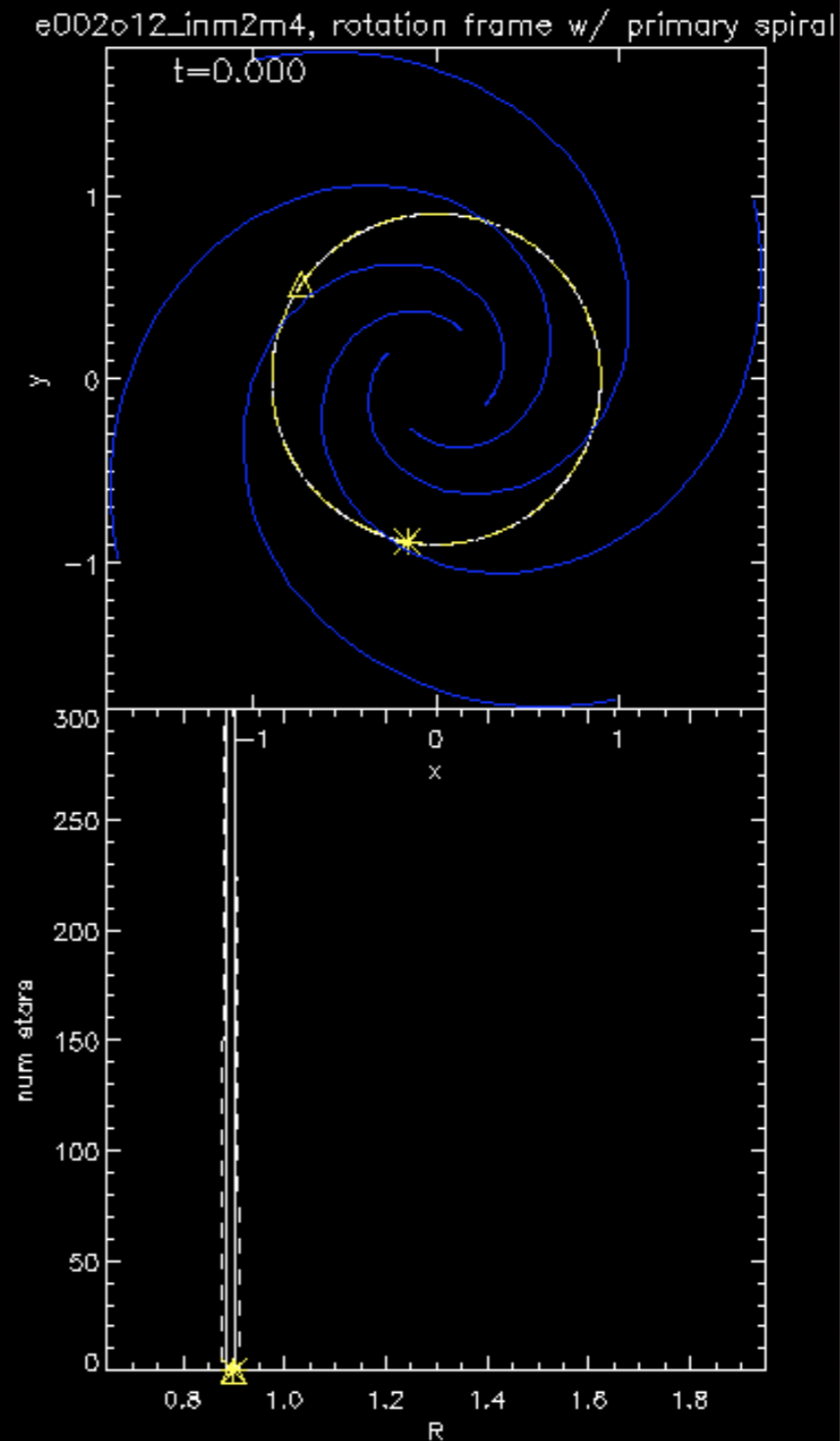
Two perturbers create stochastic regions

Multiple Spirals

m=4 just outside the ILR

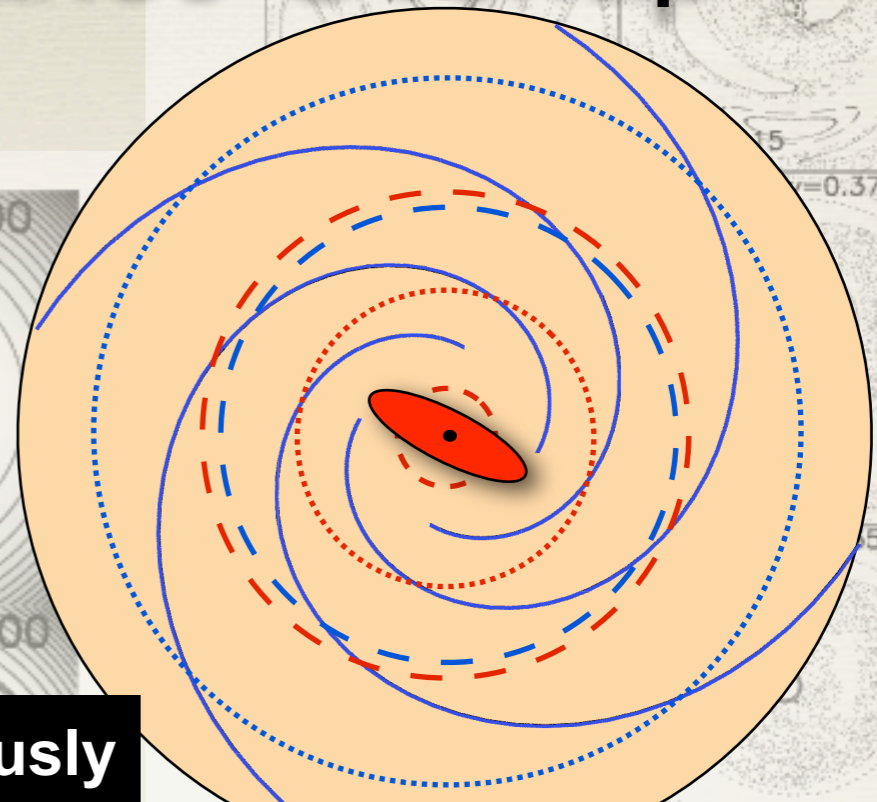
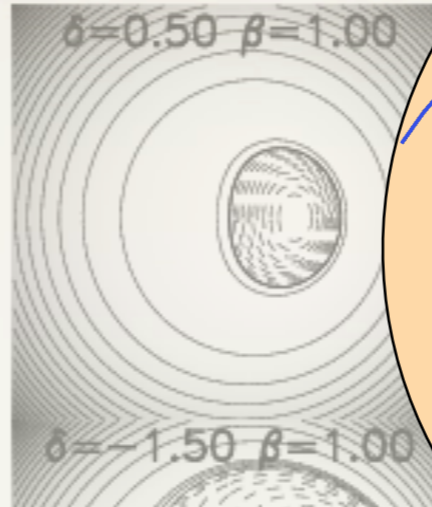
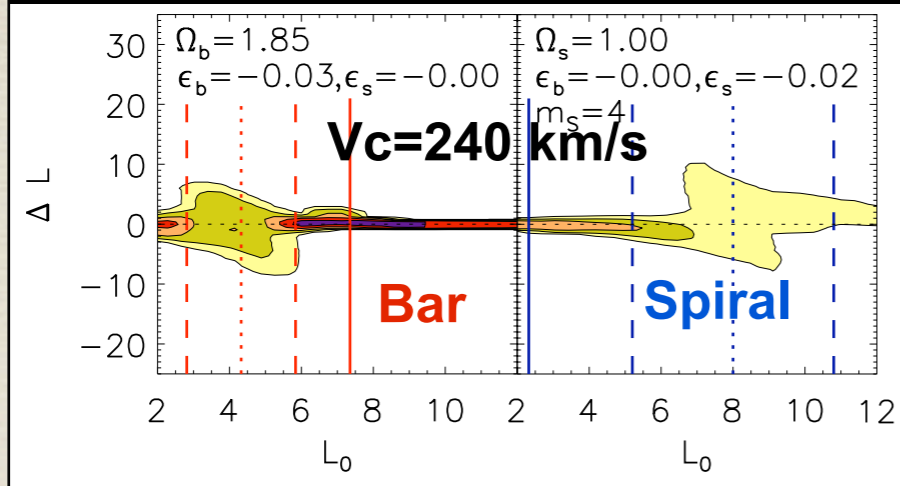


m=4 just inside the OLR

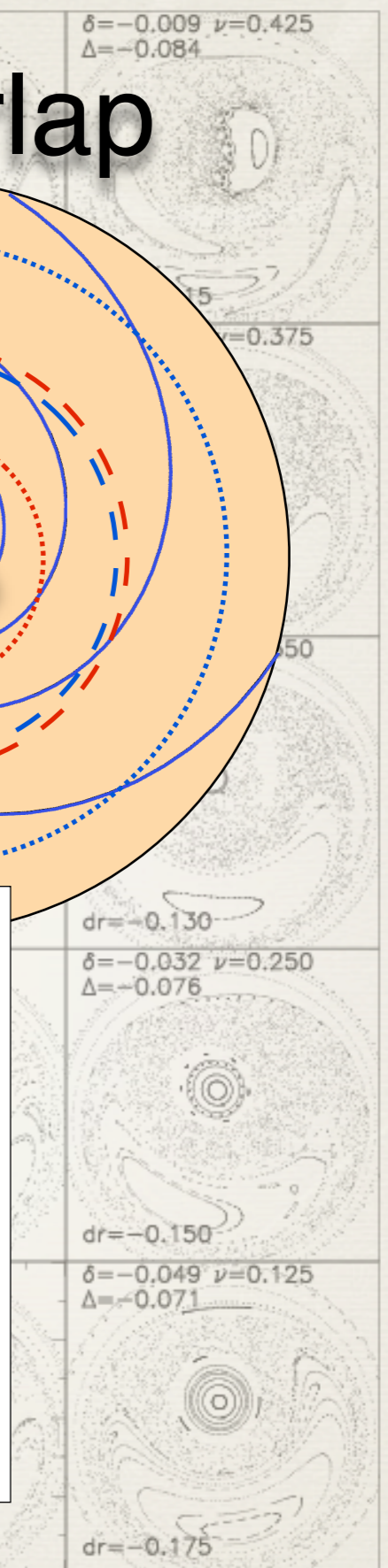
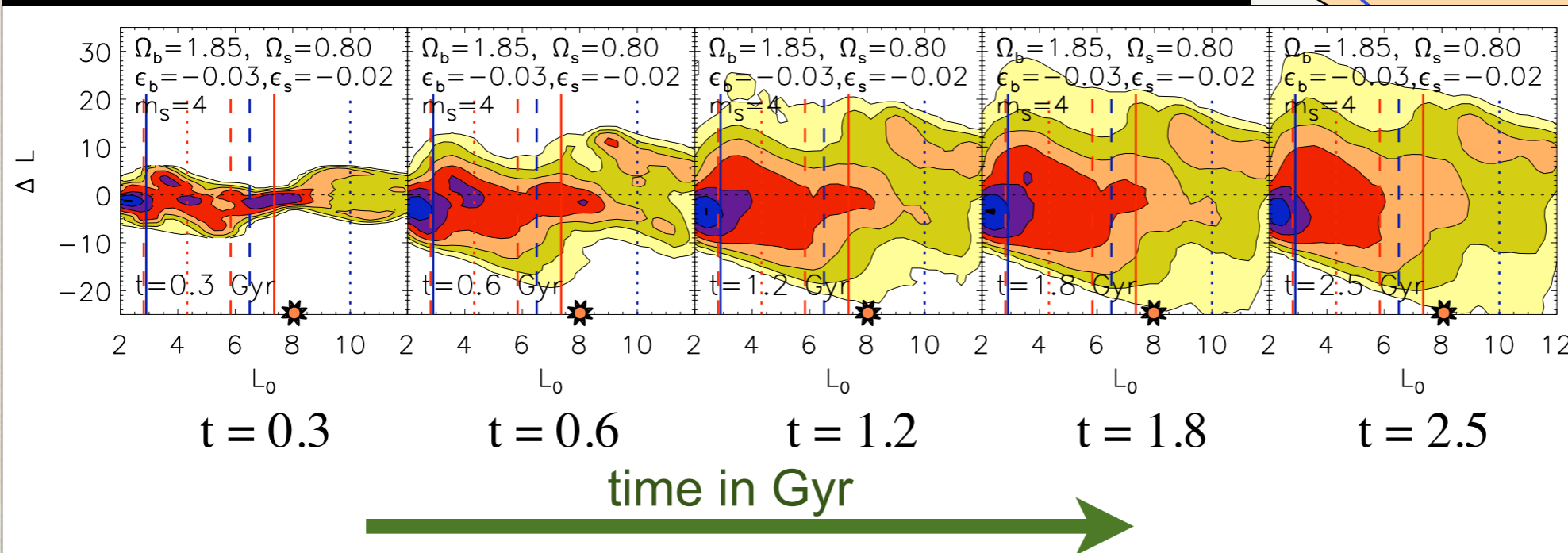


Migration due to Resonance Overlap

Single Perturber: No variation with time



Bar + Spiral Structure propagating simultaneously

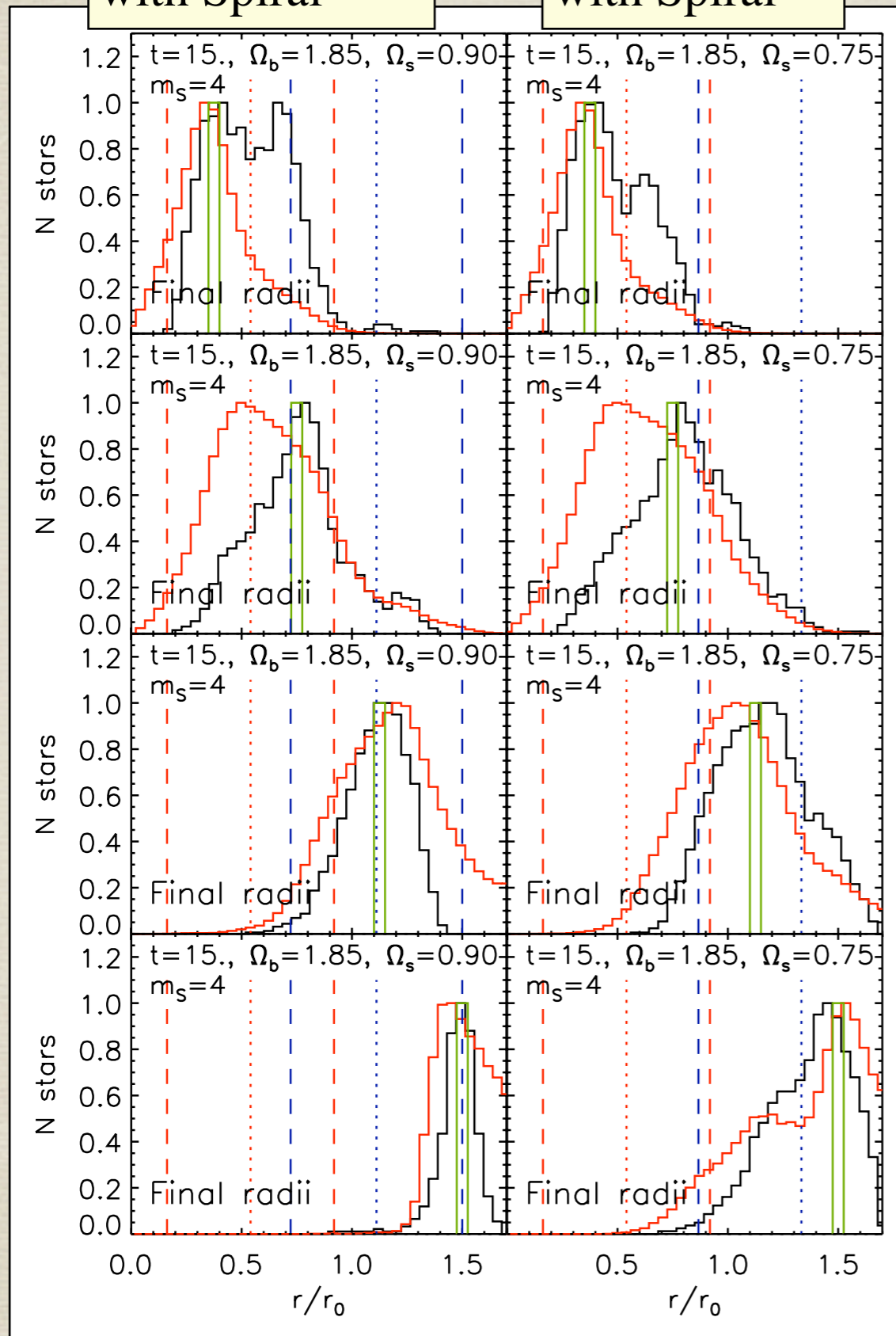


☼ Stars migrate throughout the the whole disk

0 0.2 0.4
Ω_b=1.90
ε=-0.004 β=0.0006

Near corotation
with Spiral

Near 4:1 ILR
with Spiral



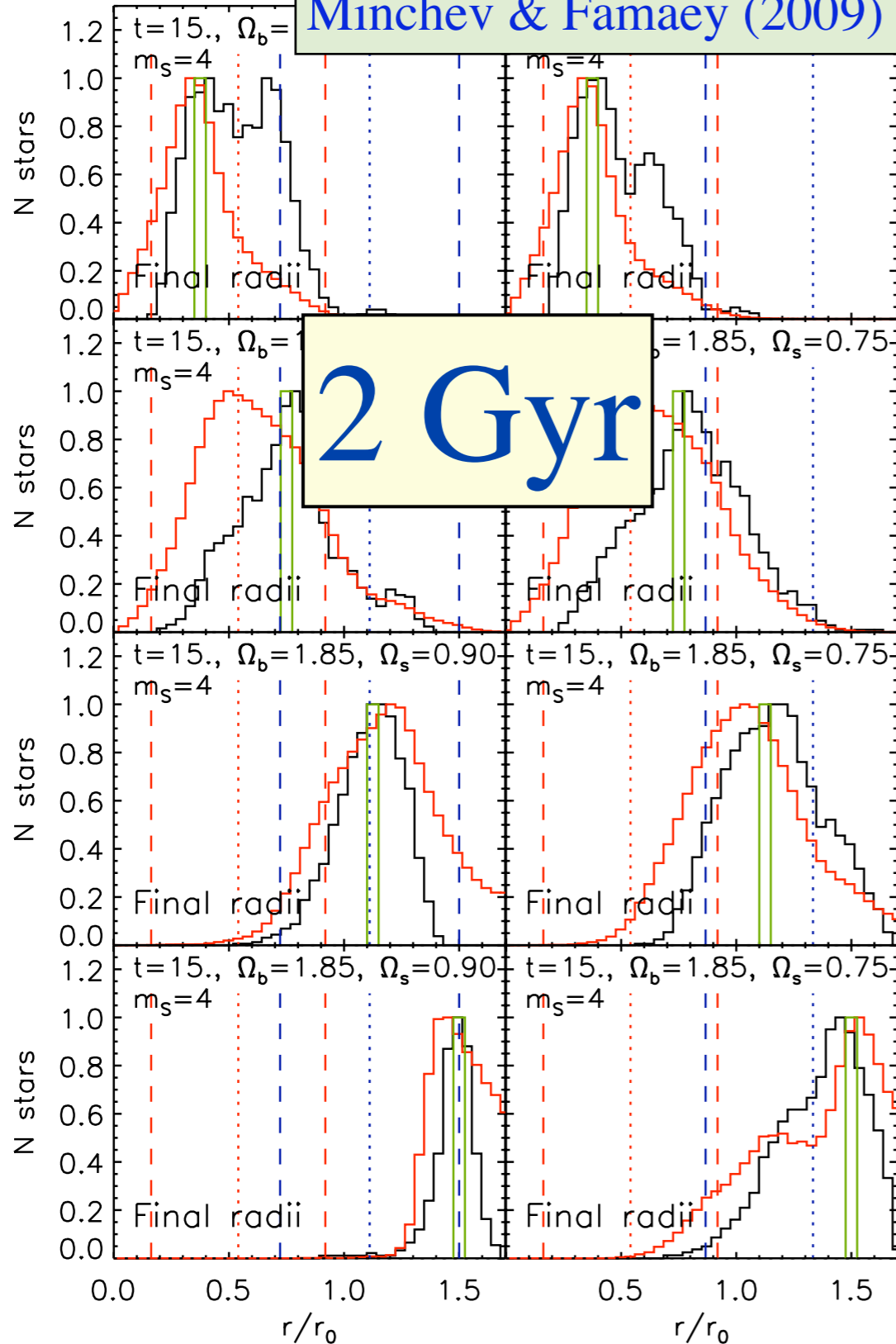
Mixing throughout the entire disk

- Distribution of home radii at $t \sim 2$ Gyr of particles starting in the range indicated by the green lines (200 pc width).

Resonance Overlap

Minchev & Famaey (2009)

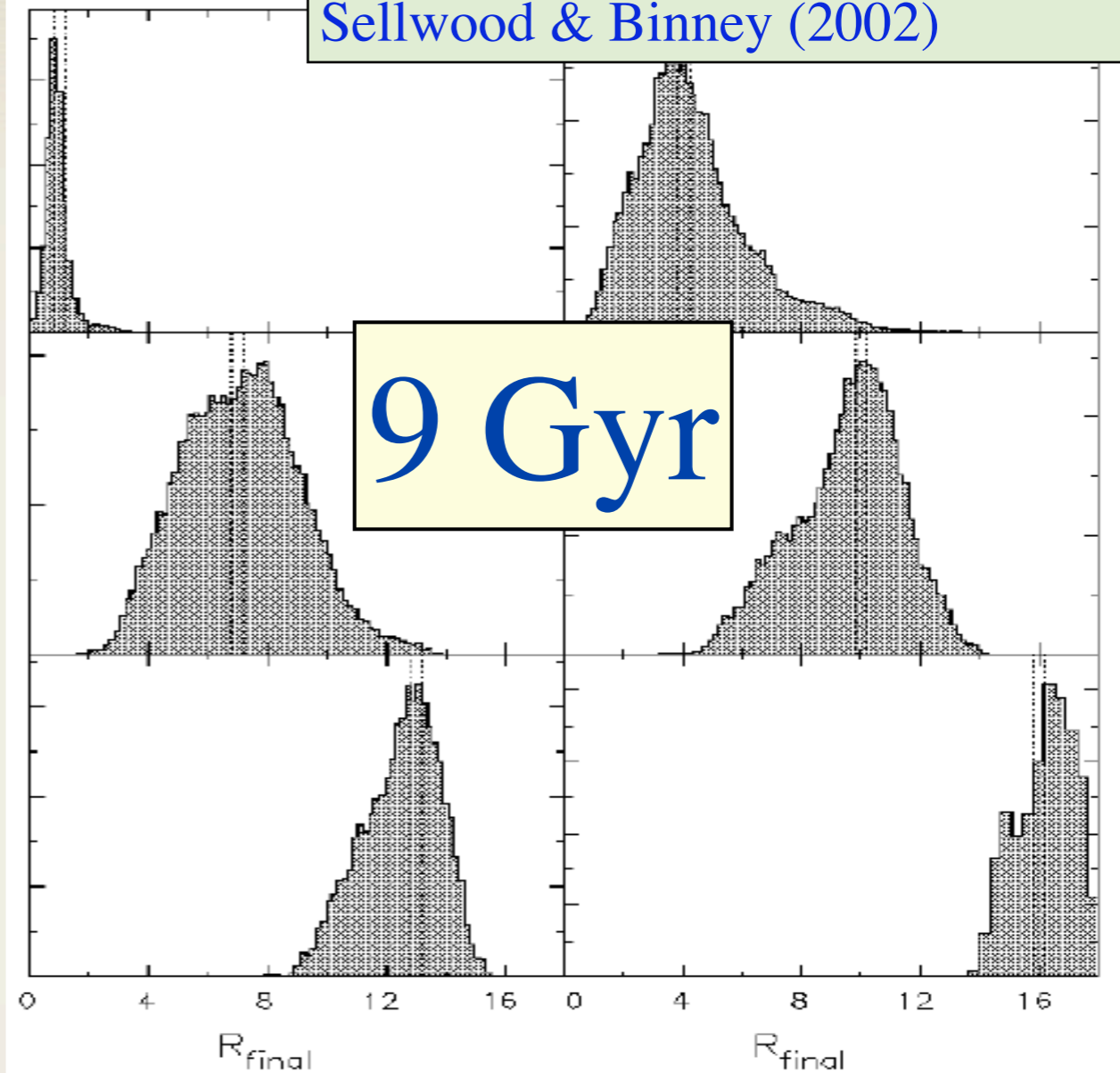
2 Gyr



Transient Spirals

Sellwood & Binney (2002)

9 Gyr

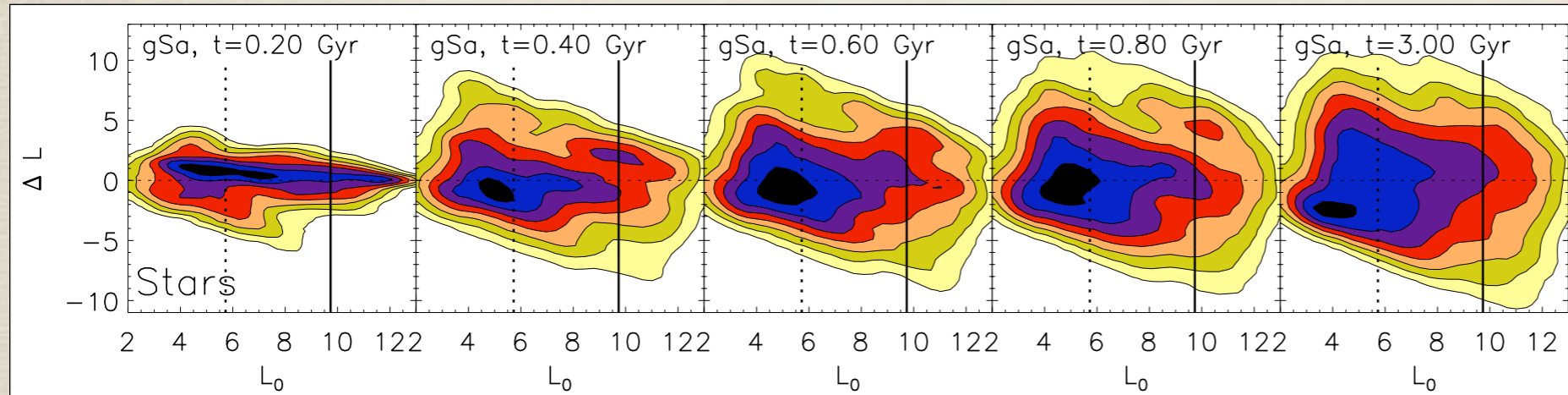


• Mixing by Resonance Overlap can be **an order of magnitude more efficient** than mixing by Transient Spirals.

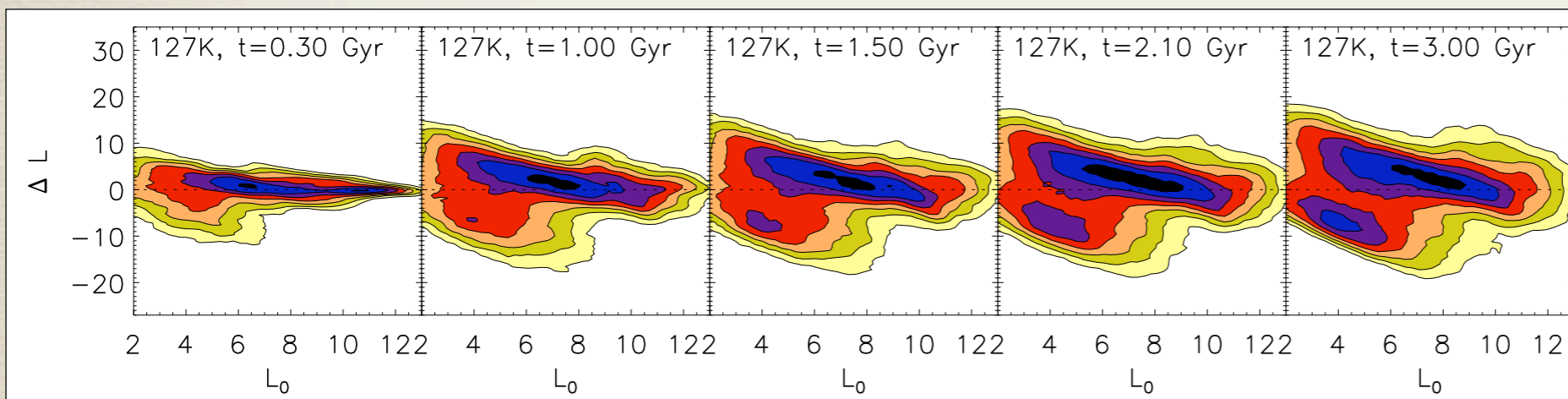
Migration from Resonance Overlap of Multiple Patterns

Confirmed in 3 independent simulation set-ups

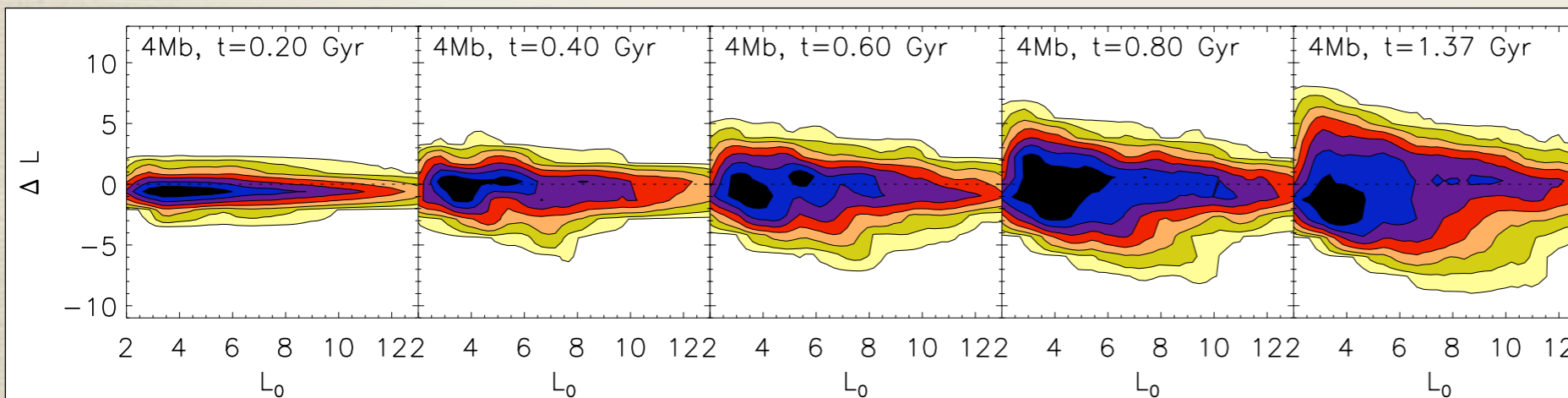
Minchev, Famaey, Combes, Di Matteo & Wozniak (2010), arXiv:1006.0484



Tree-SPH, GalMer,
Di Matteo et al. (2007)

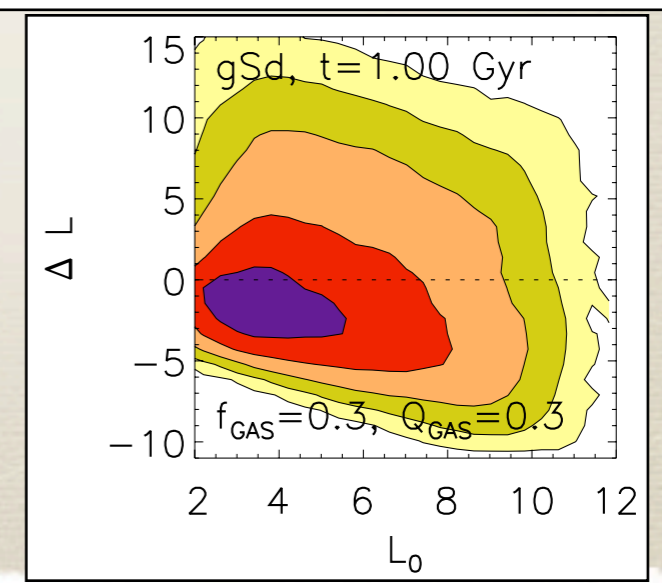
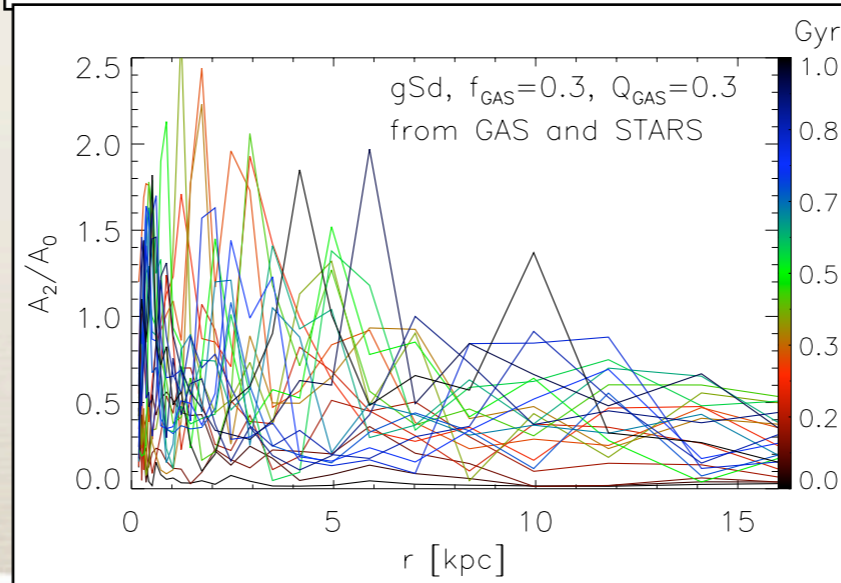
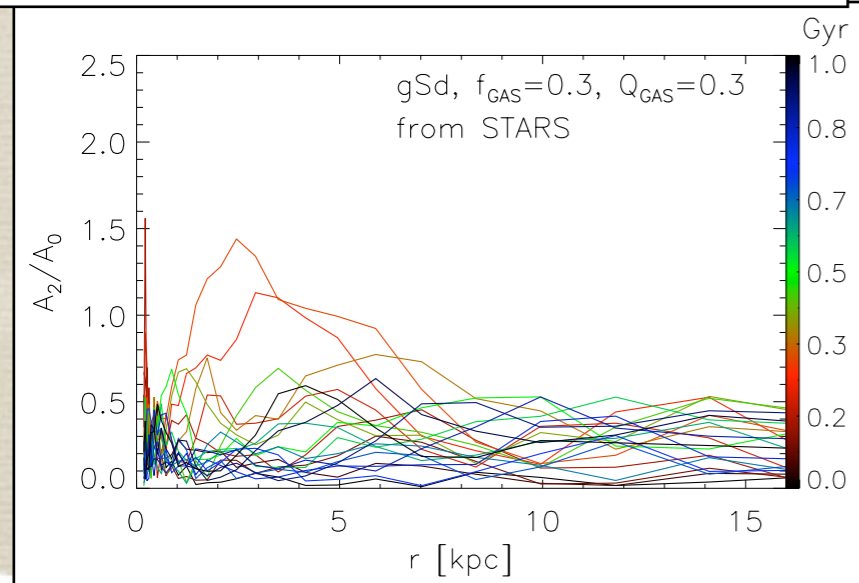
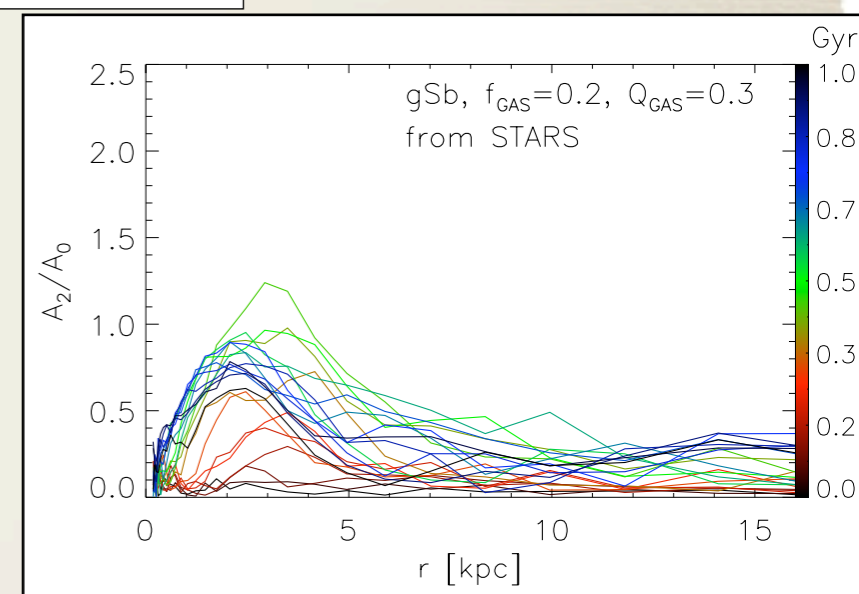
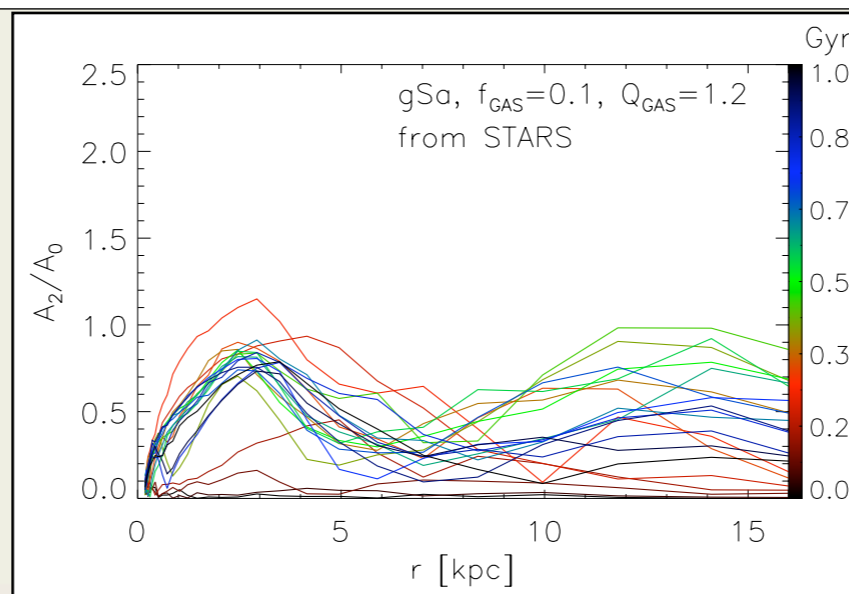
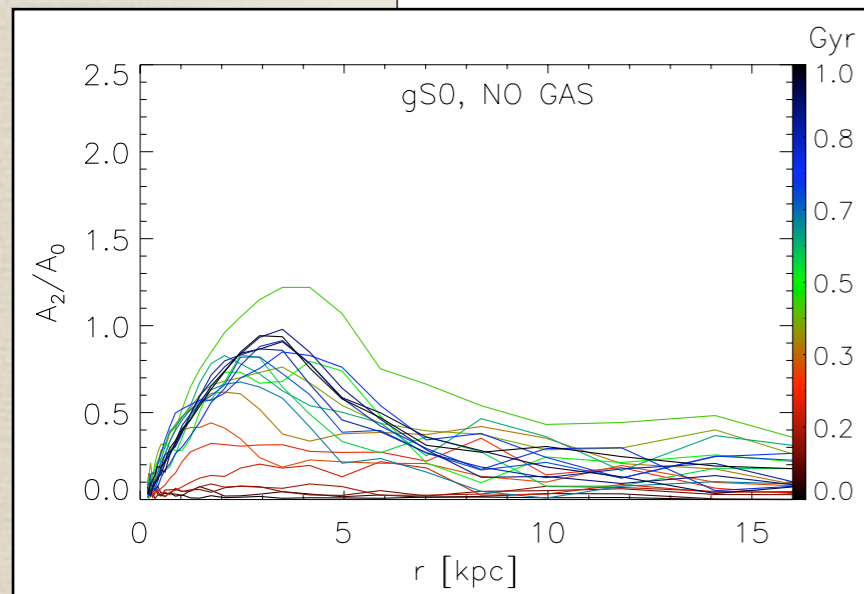
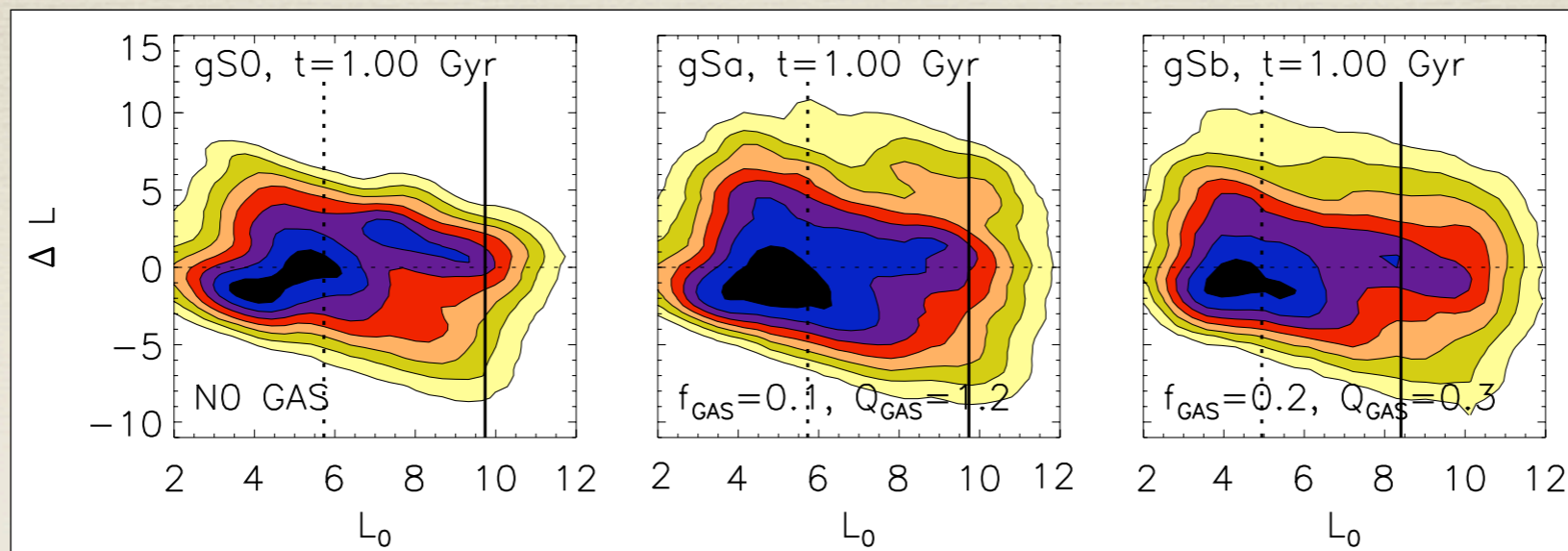


Particle-Mesh, Geneva
Group code, Wozniak &
Michel-Dansac (2009)

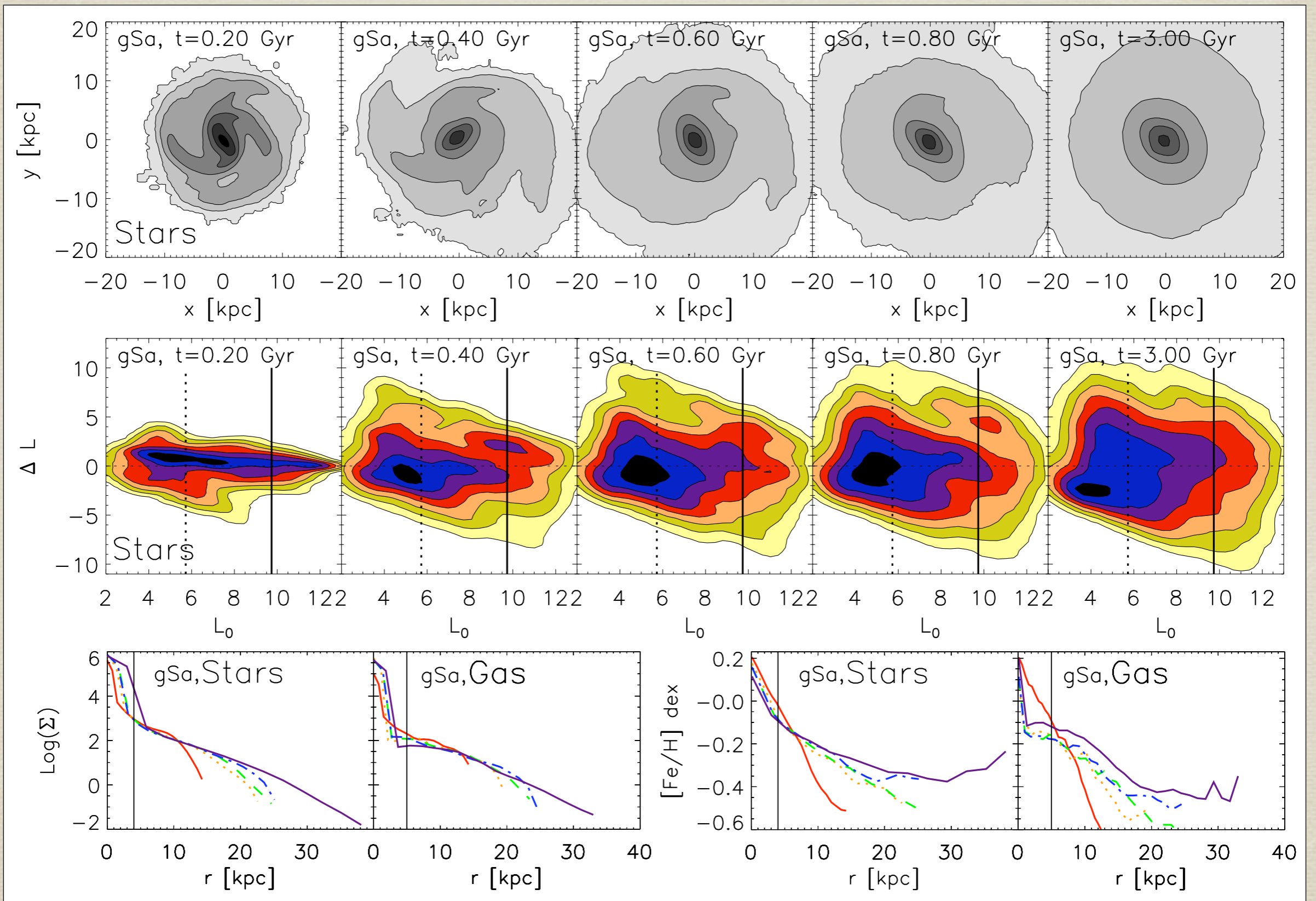


Direct N-body,
phiGRAPE (Harfst, S.
et al., 2006),
Alice Quillen on GPU

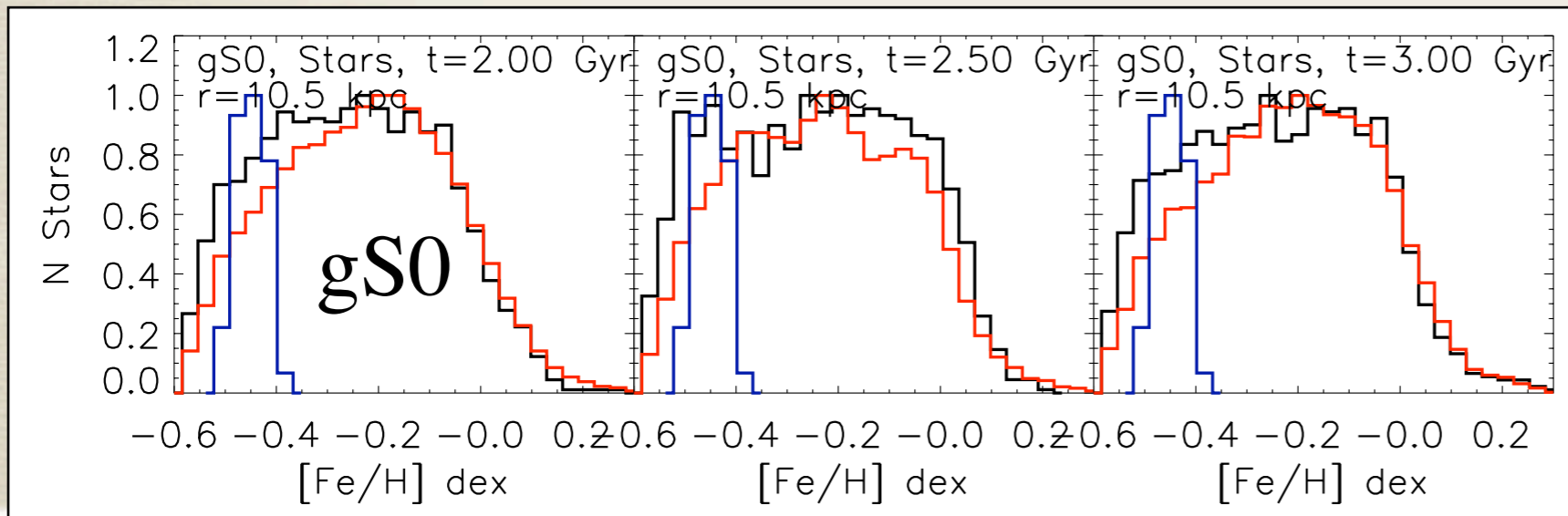
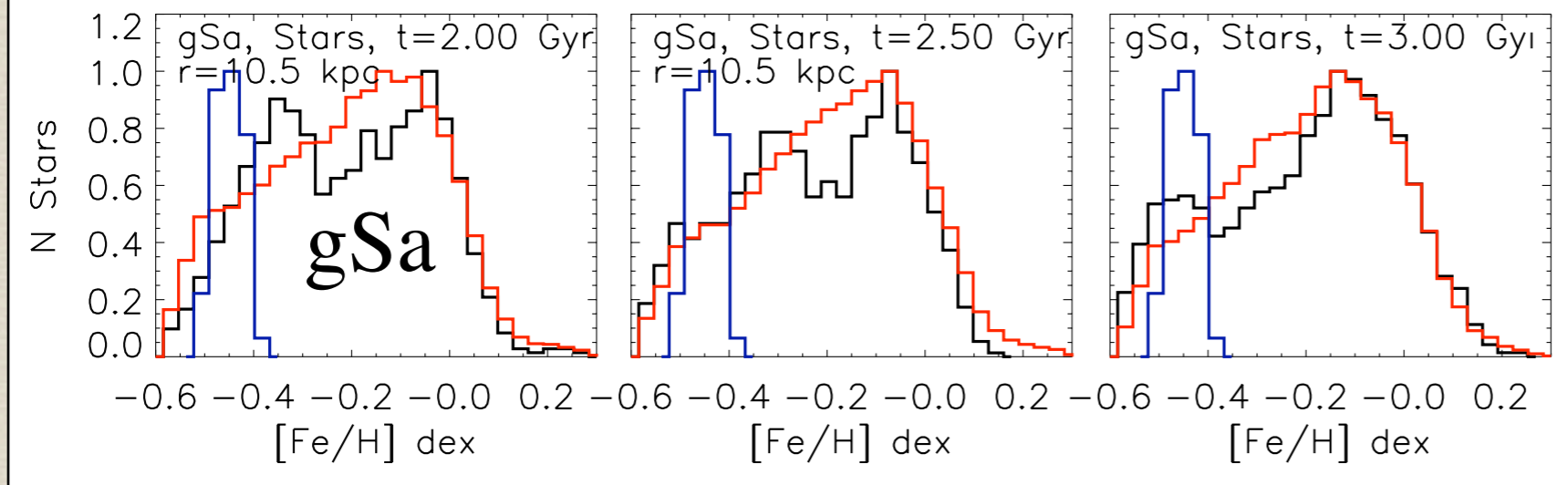
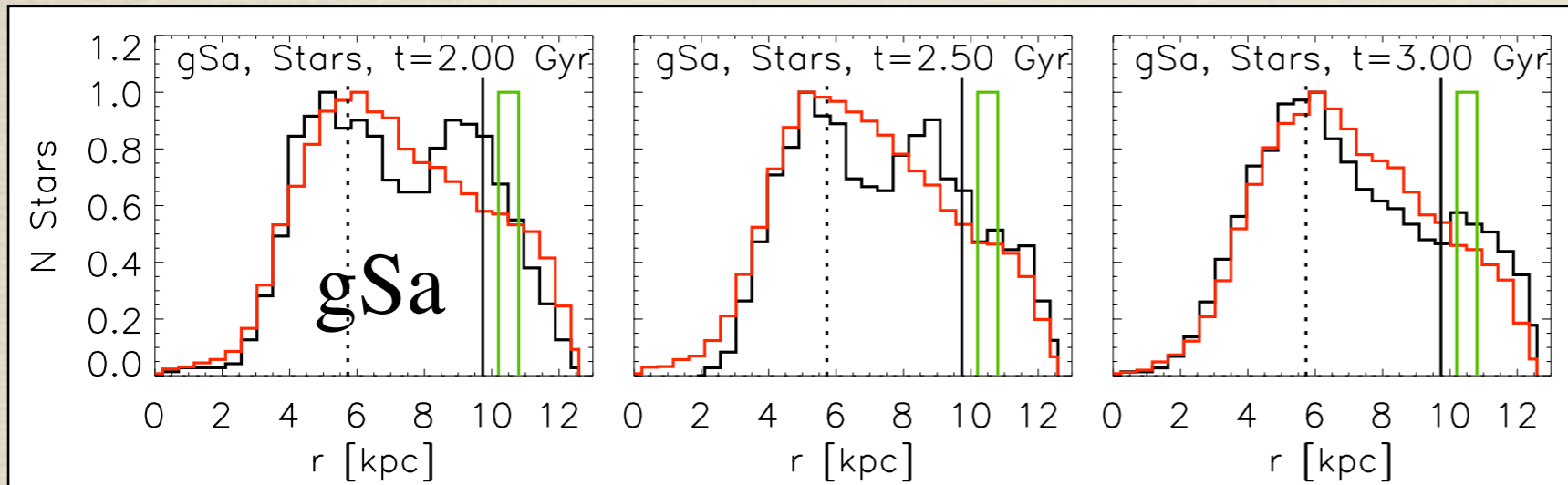
The importance of a gaseous component



GalMer giant Sa model, $V_c \sim 280$ km/s



GalMer giant Sa model, $V_c \sim 280$ km/s

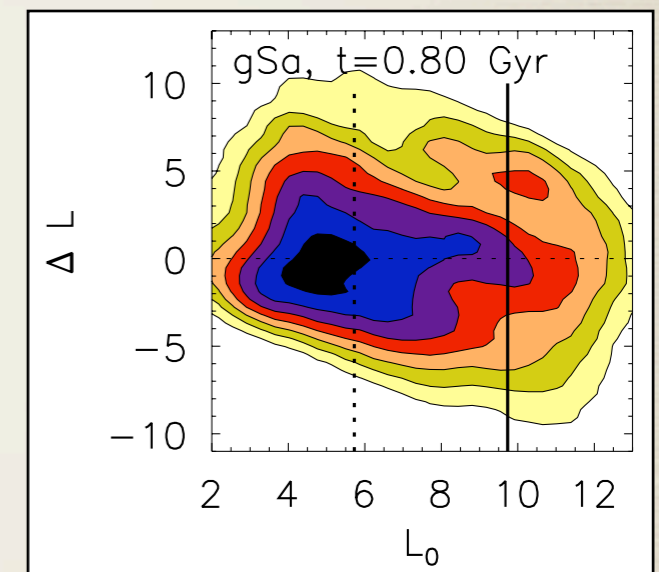


Radii Now

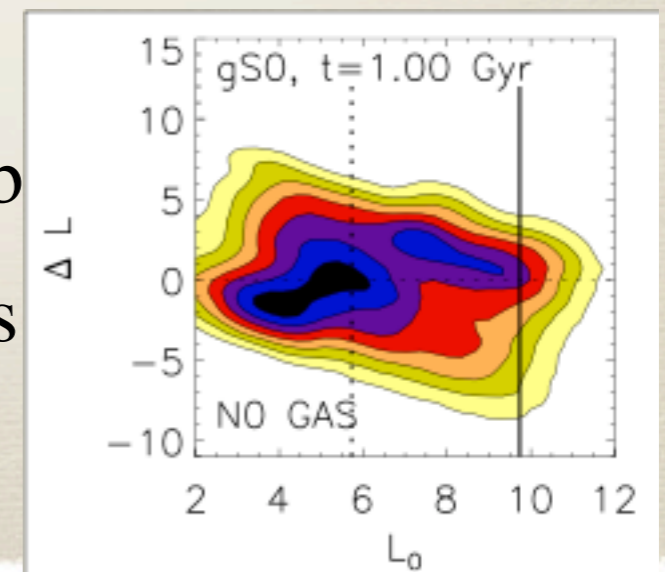
Cold orbits

Hot orbits

Initial metallicity



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's



How do we expect to identify this mechanism in the Milky Way?

- History of Milky Way bar and spiral structure currently unknown.
- Are we currently in an episode of strong mixing?
- Chemical tagging, as suggested by Ken and Joss. Up to 35 elements, 7 to 9 dimensional space. A dissolved star cluster will be a point in chemical space (HERMES, GYES).
- Look for different signatures in the density and metallicity distribution at different locations in the Galaxy (RAVE, GAIA, APOGEE).
- Extended Milky Way disk? Extensions to HERMES and GYES.
- A chemo-dynamical disk model including the effect of the Galactic bar is currently being developed (D. Pfenniger's group in Geneva).